

# Detection and Explanation of Anomalous Payment Behavior in Real-Time Gross Settlement Systems

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## RTGS Systems:

- Facilitate the settlement of financial transactions
- Settle transactions gross and (almost) real-time

## Systemic Risk:

*"The risk associated with any event that threatens the stability of a financial system as a whole" (Berndsen, et al., 2016).*

## Research Goal:

- Apply Machine Learning to analyze payment data
- Automatically identify anomalies (stress or undesired behavior)

# Anomaly Detection

Anomaly:

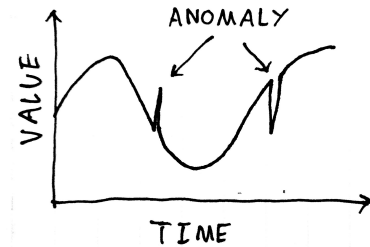
*"A pattern that does not conform to expected behavior"*  
(Chandola et al., 2009).

Unsupervised Anomaly Detection:

*The task of automatically identifying anomalies in a set of unlabeled data.*

Components:

- Model of 'normal' behavior
- Distance function



# Lossy Compression

Lossy compression preserves the most important features of data.



Original Picture



Reconstructed Picture

# Definitions

Let  $\mathcal{B} = \{b_1, \dots, b_n\}$  be a set of  $n$  banks and  $\mathcal{T} = \langle t_1, \dots, t_m \rangle$  be an ordered set of  $m$  time intervals.

We extract  $\mathcal{D} = \{\mathbf{A}^{(1)}, \dots, \mathbf{A}^{(m)}\}$  a set of  $m$  liquidity matrices from a RTGS system where each  $\mathbf{A}^{(k)} \in \mathcal{D}$  is:

$$\mathbf{A}^{(k)} = \begin{bmatrix} a_{11}^{(k)} & \cdots & a_{1n}^{(k)} \\ \vdots & \ddots & \vdots \\ a_{n1}^{(k)} & \cdots & a_{nn}^{(k)} \end{bmatrix} \quad (1)$$

Each element  $a_{ij}^{(k)}$  is the liquidity flow between  $b_i$  and  $b_j$  at  $t_k$ .

Liquidity Vector:

$$\mathbf{a}^{(k)} = [a_{11}^{(k)}, \dots, a_{n1}^{(k)}, \dots, a_{1n}^{(k)}, \dots, a_{nn}^{(k)}]^T \quad (2)$$

# Anomaly Detection Task

Let  $\mathcal{M}$  be a lossy compression model. We measure the reconstruction error of  $\mathbf{a}^{(k)}$  after its compressed and reconstructed by  $\mathcal{M}$  by:

$$\text{RE}(\mathbf{a}^{(k)}) = \frac{1}{2} \|\hat{\mathbf{a}}^{(k)} - \mathbf{a}^{(k)}\|_2^2 \quad (3)$$

Accordingly, we classify  $\mathbf{a}^{(k)}$  by:

$$h(\mathbf{a}^{(k)}) = \begin{cases} 1 & \text{if } \text{RE}(\mathbf{a}^{(k)}) \geq \epsilon \\ 0 & \text{otherwise} \end{cases} \quad (4)$$

Here,  $\epsilon > 0$  is a threshold.

We employ a three-layered autoencoder to compress and reconstruct liquidity vectors. The autoencoder can be defined by two functions:

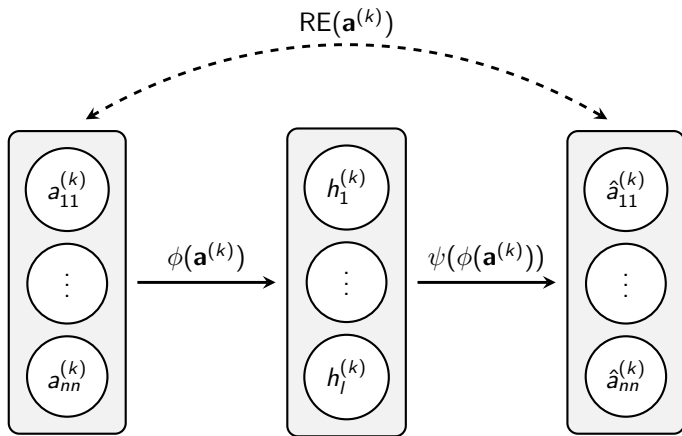
Encoder function  $\phi$ :

$$\phi(\mathbf{a}^{(k)}) = f^{(l)}(\mathbf{W}_1 \mathbf{a}^{(k)} + \mathbf{b}_1) \quad (5)$$

Decoder function  $\psi$ :

$$\psi(\phi(\mathbf{a}^{(k)})) = g^{(n^2)}(\mathbf{W}_2 \phi(\mathbf{a}^{(k)}) + \mathbf{b}_2) \quad (6)$$

# Autoencoder Architecture



# Model Learning

Parameters  $\theta = \{\mathbf{W}_1, \mathbf{W}_2, \mathbf{b}_1, \mathbf{b}_2\}$  are estimated from historic liquidity vectors. We do this by minimizing the following cost function:

$$\mathcal{J}(\theta) = \frac{1}{2m} \sum_{k=1}^m \|\psi(\phi(\mathbf{a}^{(k)})) - \mathbf{a}^{(k)}\|_2^2 + \frac{\lambda}{2} \sum_{i=1}^2 \|\mathbf{W}_i\|_F^2 \quad (7)$$

Here,  $\lambda$  is a regularization parameter.

We apply stochastic gradient descent in conjunction with back-propagation to solve this optimization problem: I.o.w an optimization algorithm.

# Experimental Setup

## Payment Data:

- 2.3 million client payments from TARGET2-NL
- Jan 2014 - Oct 2015
- Aggregated over 4,680 consecutive hours
- 20 largest banks

## Two autoencoders:

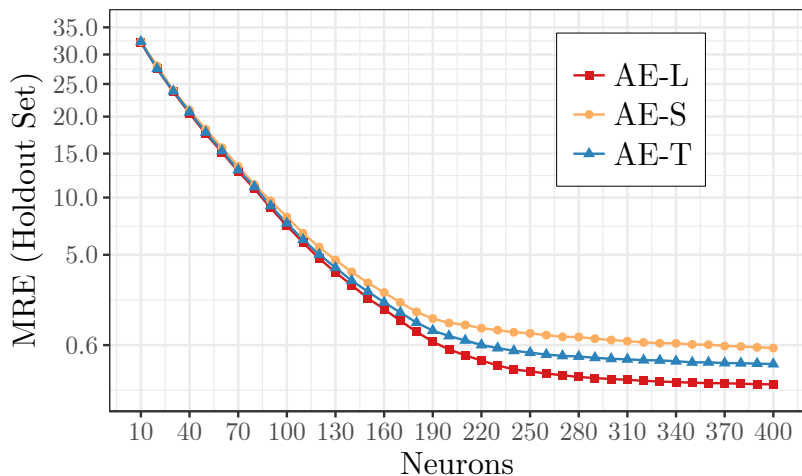
- Linear (AE-L) with (linear/linear) activations
- Non-linear (AE-S) with (sigmoid/linear) activations

## Data partitioning:

- Holdout set (2 months)
- Training set (16 months)
- Test set (4 months)

# Grid search (1/2)

The number of neurons was optimized by a grid search.



# Commercial Bank Run Simulation

Choose a bank  $b_i$  and increase its outflow to each  $b_j \in \mathcal{B}$  over time:

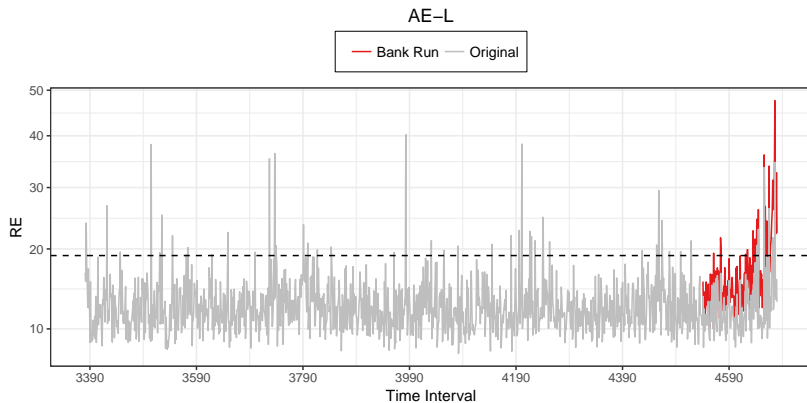
$$a_{ij}^{(k)} := a_{ij}^{(k)} + c_{ij}^{(k)} d_{ij}^{(k)} \quad (8)$$

where:

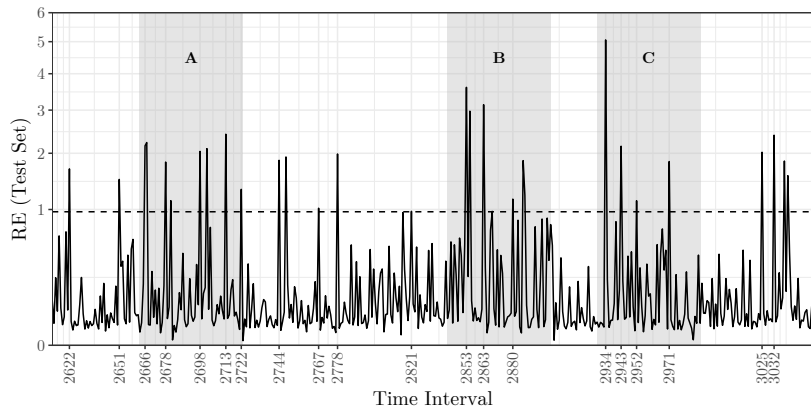
- $c_{ij}^{(k)} \sim B(1, p_{ij}^{(k)})$  determines if liquidity is added.
- $d_{ij}^{(k)} \sim \text{Exp}(\delta_{ij}^{(k)})$  is the amount of additional liquidity.

		Multipliers				
	Rate	Duration	$p_s$	$p_e$	$\delta_s$	$\delta_e$
Baseline	2	140	1	2	0.1	0.01

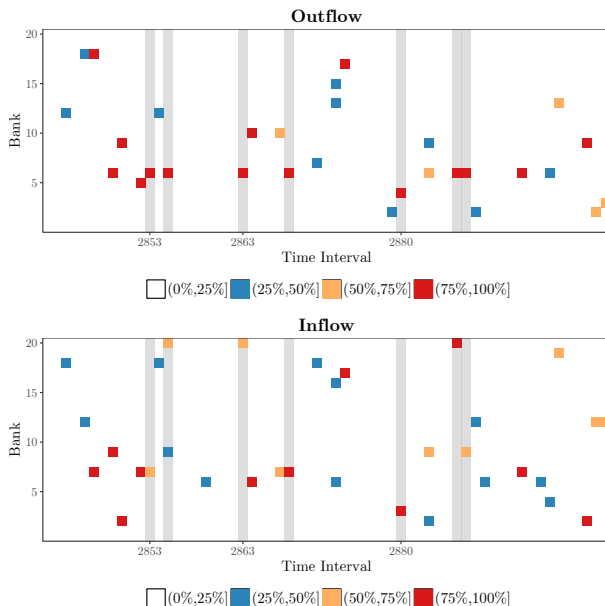
# Baseline Simulation of AE-L



# Anomalies in real data (1/3)



# Anomalies in real data (2/3)



# Anomalies in real data (3/3)

Bank run did not follow 'normal' pattern because of:

- Initially continuous outflow.
- Part of the 'gaps' had no payments (no liquidity, clients no access to accounts).
- Increased flows still considered 'normal'.

# Conclusions

- Autoencoder can detect anomalous flows reasonably well.
- Start of bank run well detected.
- However, part of the anomalous flows during bank run missed.

# Questions?