Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix

# Housing, Debt, and the Marginal Propensity to Consume

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CEPR workshop, Bank of Finland, October 22, 2015

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Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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Motivat	ion				

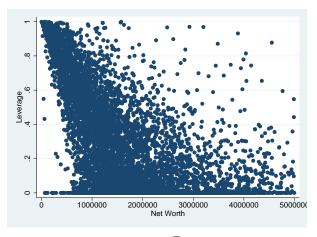
- What determines the marginal propensity to consume (MPC)?
  - Fundamental in macroeconomics
    - Aggregate demand
  - Highly policy relevant
    - Household debt overhang
    - Effect of stimulus policy and austerity
- How important are household balance sheets for the MPC?

Heterogeneity

Introduction ○●○○○○	Empirical Evidence	Model	Results 00000000000	Conclusion o	Appendix 0000
Heterog	eneity in Ho	busing Leve	erage		

0.2% Random Sample of the Data

#### ▶ Leverage



$$ev_t = \frac{B_t}{H_t}$$

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Introduction	Empirical Evidence	Model ooooooooooo	Results 00000000000	Conclusion O	Appendix 0000
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## Balance sheets and the MPC

### Existing Theory

- Buffer stock saving models (Carroll (1992; 1997))
  - MPC declines monotonically in wealth (concavity)
  - Key: degree of impatience, income uncertainty
- Two-asset models (Kaplan & Violante 2014)
  - Wealthy hand-to-mouth (HtM)
  - Key: high-return illiquid asset
- Recent empirical evidence
  - Mian & Sufi (2013): ZIPs with more levered HH had higher MPC
  - Kaplan & Violante (2014): 30% of U.S. HH are wealthy HtM

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion o	Appendix 0000
Our Pap	oer				

- Lessons from recent evidence
  - MPC seems declining in wealth and related to leverage
  - Housing seems important
    - A substantial fraction of wealth, but illiquid

• Gap: a micro-founded model with credible implications about MPC

- useful for quantitative evaluation of macro questions with micro data e.g. the effect of credit contraction/expansion
- Contribution of this study:
  - new evidence about leverage and MPC at the micro level
  - a consumption-saving life cycle model with endogenous leverage
    - matches the life cycle profiles of household balance sheets
    - generates the relation between MPC and leverage seen in the data

Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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## Debt and consumption

- Dynan (2012), Mian et al (2013)
- Eggertsson and Krugman (2012), Guerrieri and Lorenzoni (2011)

## Excess sensitivity

- Baker (2014; 2015); Parker (2015)
- Carroll et al (2014), Kaplan and Violante (2014)
- Life cycle choices
  - Gourinchas and Parker (2002), Cagetti (2003)
  - Fernandez-Villaverde and Krueger (2011), Yang (2009)
- Solving dynamic stochastic optimization problem
  - Carroll (2006)
  - Iskhakov et al (2014), Hintermaier and Koeniger (2010)

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Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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- Leverage and MPC in micro data
  - Data
  - Leverage and consumption response to wealth changes
- A consumption-saving life cycle model
  - explicit modeling of housing and debt
  - liquid and illiquid assets (cf. Kaplan and Violante 2014)

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- Model vs. data and implications for MPC
- Policy implications
  - A sudden credit contraction
  - A permanently lower LTV-limit

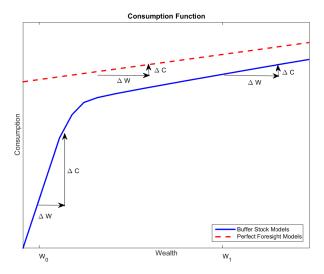
Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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Data					

- Norwegian registry data 2005-2011
  - Household level data in normal times
  - Knowledge about the structure and the dynamics of balance sheets (not available in PSID)
- Full balance sheet
  - Housing
  - Debt
  - Financial assets
    - Deposits
    - Bonds
    - Stocks
    - Mutual funds
  - Income
- Imputed consumption
- Detailed household characteristics
  - Area, education, marital status, family type and size, etc

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Introduction	Empirical Evidence	Model ०००००००००००	Results 00000000000	Conclusion O	Appendix 0000

## Concavity of Consumption Function



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Introduction 000000	Empirical Evidence	<b>Model</b> 00000000000	Results 00000000000	Conclusion O	Appendix 0000
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## Mian-Rao-Sufi Type Regressions on Micro Data

Regression equation

$$\Delta C_{it} = \beta_0 + \beta_1 \Delta W_{it} + \beta_2 W_{it-1} + \frac{\beta_3 \Delta W_{it} \times W_{it-1}}{+\beta_4 lev_{it-1} + \frac{\beta_5 \Delta W_{it} \times lev_{it-1}}{+\beta_5 \Delta W_{it} \times lev_{it-1}} + \text{control variables} + \epsilon_{it}$$

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• From simple buffer-stock theory:

• 
$$\beta_3 < 0$$

•  $\beta_5 = 0$ 

 Introduction
 Empirical Evidence
 Model
 Results
 Conclusion
 Appendiation

 Mian-Sufi Type Regressions on Micro Data

 Fixed Effect

Regression equation

$$\Delta C_{it} = \beta_{0,i} + \beta_{1,i} \Delta W_{it} + \beta_2 W_{it-1} + \beta_3 \Delta W_{it} \times W_{it-1} + \beta_4 lev_{it-1} + \beta_5 \Delta W_{it} \times lev_{it-1} + \text{control variables} + \epsilon_{it}$$

- Fixed effect in slopes (FEIS)
  - Unobserved household heterogeneity (preference, expectations, etc)

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Parker (2015): MPC a persistent household trait, related to impatience

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion O	Appendix 0000

# Mian-Rao-Sufi Type Regressions on Micro Data

Dep.Var:			$\Delta C_t$	
	(1)	(2)	(3)	(4)
$\Delta W_t$	0.595*** (0.002)	0.445*** (0.002)	0.531*** (0.106)	
$W_{t-1}$	-0.012***	-0.060***	-0.096 <sup>*</sup> **	0.121***
$\Delta W_t \times W_{t-1}$	(0.000) -0.015***	(0.000) 0.003***	(0.001) 0.008***	(0.004) 0.064***
$lev_{t-1}$	(0.001)	(0.001) -0.194***	(0.001) -0.337***	(0.007) -0.747***
$\Delta W_t \times lev_{t-1}$		(0.001) 0.197***	(0.001) 0.226***	(0.008) 0.375***
Year# Ÿ# CHAR# FEIS	х	(0.002) X	(0.002) X X X X	(0.022) X X X X X
adj. $R^2$ N	0.281 1,346,844	0.309 1,346,844	0.346 1,346,264	0.231 1,191,995

Introduction	Empirical Evidence	Model 00000000000	Results 0000000000	Conclusion o	Appendix 0000
Mian-R	ao-Sufi Type	e Regressio	ons on Mic	ro Data	

Aggregation

Dep.Var:	$\Delta C_t$				
Agg. Level:	Household	Household	Municipality	County	
	(1)	(2)	(3)	(4)	
$\Delta W_t \times lev_{t-1}$	0.226***	0.375***	0.348***	0.390	
	(0.002)	(0.022)	(0.054)	(0.595)	
Baseline $W_{t-1}$	Х	X	Х	X	
Year#	Х	Х	Х	Х	
Age#	Х	Х	Х	Х	
CHAR#	Х	Х			
FEIS		Х			
adj. $R^2$	0.291	0.231	0.939	0.950	
N	1,346,844	1,191,995	2,147	95	

 Introduction
 Empirical Evidence
 Model
 Results
 Conclusion
 Appendix

 Mian-Rao-Sufi Type
 Regressions on Micro Data

 Alternative Specification

## • Controlling for wealth-to-income ratio

$$\Delta C_{it} = \beta_0 + \beta_1 \Delta W_{it} + \beta_2 \frac{W_{it-1}}{Y_{it-1}} + \beta_3 \Delta W_{it} \times \frac{W_{it-1}}{Y_{it-1}} + \beta_4 lev_{it-1} + \beta_5 \Delta W_{it} \times lev_{it-1} + \text{control variables} + \epsilon_{it}$$

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 Introduction
 Empirical Evidence
 Model
 Results
 Conclusion
 Appendix

 Mian-Rao-Sufi Type
 Regressions on Micro Data

 Alternative Specification

## • Controlling for wealth-to-income ratio

$$\Delta C_{it} = \beta_{0,i} + \beta_{1,i} \Delta W_{it} + \beta_2 \frac{W_{it-1}}{Y_{it-1}} + \beta_3 \Delta W_{it} \times \frac{W_{it-1}}{Y_{it-1}} + \beta_4 lev_{it-1} + \beta_5 \Delta W_{it} \times lev_{it-1} + \text{control variables} + \epsilon_{it}$$

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Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
	00000000000				

# Mian-Rao-Sufi Type Regressions on Micro Data

Dep.Var:			$\Delta C_t$	
	(1)	(2)	(3)	(4)
$\Delta W_t$	0.659*** (0.001)	0.521*** (0.002)	0.804*** (0.107)	•
$\frac{W_{t-1}}{Y_{t-1}}$	0.001***	-0.013***	-0.012***	0.006***
11-1	(0.000)	(0.000)	(0.000)	(0.001)
$\Delta W_t \times \frac{W_{t-1}}{Y_{t-1}}$	-0.017***	-0.010***	-0.010***	-0.002
$lev_{t-1}$	(0.000)	(0.000) -0.201*** (0.001)	(0.000) -0.253*** (0.001)	(0.002) -0.864*** (0.007)
$\Delta W_t \times lev_{t-1}$		0.167***	0.206***	0.299***
Year# Ӯ# CHAR# FEIS	х	(0.002) X	(0.002) X X X X	(0.021) X X X X X
adj. <i>R</i> <sup>2</sup> N	0.283 1,346,844	0.306 1,346,844	0.335 1,346,264	0.224 1,191,995

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion o	Appendix
Mian-R Aggregatio	ao-Sufi Type	e Regressi	ons on Mic	ro Data	

Dep.Var:	$\Delta C_t$					
Agg. Level:	Household	Household Household Mu		County		
	(1)	(2)	(3)	(4)		
$\Delta W_t \times lev_{t-1}$	0.206*** (0.002)	0.299*** (0.021)	0.306*** (0.083)	0.667 (0.597)		
Baseline $\frac{W_{t-1}}{Y_{t-1}}$	Х	Х	Х	Х		
Year#	Х	Х	Х	Х		
Age#	Х	Х	Х	Х		
CHAR#	Х	Х				
FEIS		Х				
adj. $R^2$	0.335	0.224	0.936	0.949		
N	1,346,264	1,191,995	2,147	95		

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion o	Appendix 0000
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## The Role of Housing Leverage

### • $\beta_5 > 0$

- Statistically significant
- Economically important
  - Consider a household who moved from a small apartment to a big house

$$lev_{t-1} = 0.3 \longrightarrow lev_t = 0.8$$
$$\Delta\left(\frac{dC_t}{dM_t}\right) \approx 0.10$$

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- Leverage is related to MPC over and above wealth
- WHY?

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion o	Appendix 0000
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## The Role of Housing Leverage

- In the presence of housing
  - total wealth is not a good proxy for the proximity to the liquidity constraint
  - but leverage is
- Housing plays several roles in affecting consumption
  - Illiquid wealth
    - In the short run, consumption is more affected by liquid wealth
    - (S,s)-rule over housing
  - Consumption good
    - complementarity with non-housing consumption
  - Collateral
- Will a consumption-saving model with housing generate similar portfolio choices over the life cycle as in the data?
  - And what will it say about the link between leverage and MPC?

Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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Ingredie	ents				

- Two assets
  - Housing H and financial wealth M
  - No asset price uncertainty
- Consumption  $\tilde{C}(C, S)$ 
  - $\bullet\,$  Non-housing consumption C and housing service flow S
  - Renters purchase S, homeowners derive utility from owning  $S = \zeta H$
- Housing transaction cost
  - Purchase  $\kappa_p$
  - Sale  $\kappa_s$
- Other ingredients
  - Income profiles: growth  $\{\Gamma_a\}_{a=27}^{90}$  and idiosyncratic risk  $\{\sigma_{\xi,a}^2\}_{a=27}^{90}$ ,
    - $\{\sigma^2_{\psi,a}\}^{90}_{a=27}$
  - Borrowing constraint  $\mu_V$ ,  $\mu_Y$ ,  $\mu_U$
  - Conditional probability of survival  $\{p_a^S\}_{a=27}^{90}$
  - Family composition  $\{N_a^{Adult}\}_{a=27}^{90}, \{N_a^{Children}\}_{a=27}^{90}$
  - Bequest motives

Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
000000		○●○○○○○○○○○	00000000000	o	0000
Setup Preferences					

• CES consumption index

$$\tilde{C}_a = \left[ \alpha_a^{\frac{1}{\theta}} C_a^{\frac{\theta-1}{\theta}} + (1 - \alpha_a)^{\frac{1}{\theta}} S_a^{\frac{\theta-1}{\theta}} \right]^{\frac{\theta}{\theta-1}}$$

Weight on non-housing consumption

$$\alpha_a \propto \alpha \exp\{f_a N_a^{Adult} + f_c N_a^{Children}\}$$

CRRA utility

$$u(\tilde{C}_a) = \frac{\tilde{C}_a^{1-\rho}}{1-\rho} \qquad \rho > 1$$

Bequest

$$u^{b}(W_{a+1}) = \varphi \frac{W_{a+1}^{1-\rho}}{1-\rho},$$

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Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
000000		○○●○○○○○○○○○	00000000000	o	0000
Setup	ess				

Permanent-transitory type of income process

$$Y_a = P_a \Xi_a$$
$$P_a = \Gamma_a P_{a-1} \Psi_a$$

#### Notation

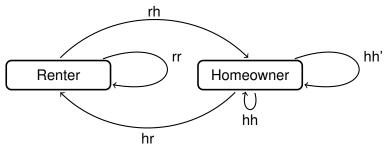
- Y<sub>a</sub> after-tax income
- *P<sub>a</sub>* permanent component of income
- $\Xi_a$  transitory component of income
- $\Gamma_a$  deterministic growth rate
- $\Psi_a$  shock to permanent income
- Permanent and transitory shocks are log-normal

$$\begin{aligned} \xi_a &= \log \Xi_a \sim N(-\sigma_{\xi,a}^2/2, \sigma_{\xi,a}^2) \\ \psi_a &= \log \Psi_a \sim N(-\sigma_{\psi,a}^2/2, \sigma_{\psi,a}^2) \end{aligned}$$

Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
000000		○○○●○○○○○○○	00000000000	O	0000
Setup					

• Discrete choices: *rr*, *rh*, *hr*, *hh*, *hh*'

Renters and Homeowners



- Transaction costs related to housing
  - $\kappa_p, \kappa_s$  Transaction costs of housing purchase and sale

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Introduction	Empirical Evidence	Model ○000●000000	Results 00000000000	Conclusion o	Appendix
Setup					

Setup Borrowing Constraints

Loan to value

$$A_a \ge -\mu_V H_{a+1}$$

Loan to income

$$A_a \ge -\mu_Y P V_a$$

where  $PV_a$  is expected income in the future

Unsecured borrowing

$$A_a \ge -\mu_U P_a$$

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• Borrowing rate  $r_b > \text{Risk}$  free rate r

Introduction	Empirical Evidence	Model ○0000●○○○○○	Results 00000000000	Conclusion o	Appendix 0000
Setup Households	' Problem				

$$\max u(\tilde{C}_{a_0}) + E_{a_0} \left[ \sum_{a=a_0+1}^T \beta^{a-a_0} \left( p_a^S u(\tilde{C}_a) + (1-p_a^S) u^b(W_a) \right) \right]$$

subject to

$$\int M_a - C_a - S_a \qquad rr$$

$$M_a - C_a - S_a - (1 + \kappa_p)H_{a+1} \qquad rh$$

$$A_a = \left\{ \begin{array}{ll} M_a - C_a + (1 - \kappa_s - \delta)H_a \\ hr \end{array} \right.$$

$$M_a - C_a + (1 - \kappa_s - \delta)H_a - (1 + \kappa_p)H_{a+1} \qquad hh' \\
 M_a - C_a \quad (H_{a+1} = (1 - \delta)H_a) \qquad hh$$

$$M_{a+1} = \begin{cases} (1+r)A_a + Y_{a+1} & A_a \ge 0\\ (1+r_b)A_a + Y_{a+1} & A_a < 0 \end{cases}$$
$$W_a = M_a + H_a$$

Introduction 000000	Empirical Evidence	Model	Results 00000000000	Conclusion o	Appendix 0000
Estimat	rion				

### • First step (external calibration)

- Income process
  - Deterministic growth rate
  - Age-varying idiosyncratic risk 

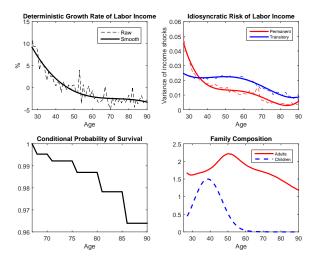
     BPP
- Conditional probability of survival
- Household composition
- Transaction cost, interest rates, minimum housing, depreciation rate

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- Initial distribution of balance sheets Initial Dist
- Second step (preference estimation)
  - Preference parameters:  $\rho$ ,  $\beta$ ,  $\theta$ ,  $\alpha$ ,  $\zeta$ ,  $\varphi$ ,  $f_a$ ,  $f_c$
  - Simulated method of moments

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Introduction	Empirical Evidence	<mark>Model</mark> ○○○○○○ <b>○●○○○</b>	Results 00000000000	Conclusion O	Appendix 0000

## **External Calibration**



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Introduction	Empirical Evidence	Model ○○○○○○○○○○○○	Results ooooooooooo	Conclusion O	Appendix 0000

## First Step Parameters

Estimates	Parameter	Value	Target/Source
First Step			
Demographics			
Lifespan	T	90	
Conditional probability of survival	$\{p_a^S\}$		SSB
Income process			
Permanent income growth rate	$\{\Gamma_t\}$		SSB
Variance of permanent income	$\{\sigma_{\Psi,t}\}$		SSB
Variance of transitory income	$\{\sigma_{\Xi,t}\}$		SSB
Borrowing			
Risk free rate	r	0.016	Norges Bank
Borrowing rate	$r_b$	0.054	Norges Bank
Maximum loan to value ratio	$\mu_V$	0.90	Norges Bank
Maximum debt to lifetime income ratio	$\mu_Y$	0.25	
Housing market			
Depreciation rate	δ	2%	
Transaction cost of purchase	$\kappa_p$	0.025	
Transaction cost of sale	$\kappa_p$	0.025	
Minimum housing	$\underline{h}$	8.2	SSB

Introduction	Empirical Evidence	Model ○○○○○○○○○●○	Results 00000000000	Conclusion o	Appendix 0000
Estimat Second Ste					

- Target ( $64 \times 3$  moments):
  - Median net worth  $\{A_a\}_{a=27}^{90}$
  - Housing  $\{H_a\}_{a=27}^{90}$
  - Homeownership rate  $\{O_a\}_{a=27}^{90}$
- Method (8 parameters): method of simulated moments
  - Simulated profiles  $\{A_a^s\}_{a=27}^{90}, \{H_a^s\}_{a=27}^{90}, \{O_a^s\}_{a=27}^{90}$
  - Distance between the profiles in the data and in the simulated data is the smallest

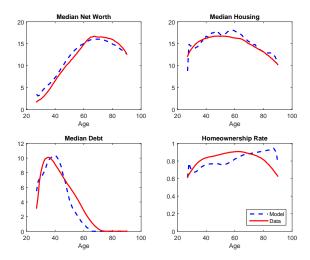
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Introduction	Empirical Evidence	<mark>Model</mark> ○○○○○○○○○○○	Results 0000000000	Conclusion O	Appendix 0000	

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Estimates	Parameter	Value
Second Step		
Preference		
Initial weight on consumption	$\alpha$	0.55
Adults' impact on consumption weight	$f_a$	0.47
Children's impact on consumption weight	$f_a$	0.12
Discount factor	$\beta$	0.93
Coefficient of relative risk aversion	ho	1.20
Elasticity of substitution	$\theta$	0.49
Utility of owning	ζ	0.09
Bequest weight	$\varphi$	12.3

Introduction	Empirical Evidence	Model 00000000000	Results •••••••	Conclusion o	Appendix 0000
Life Cyc Model vs. D	cle Profiles				



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Introduction

Empirical Evidence

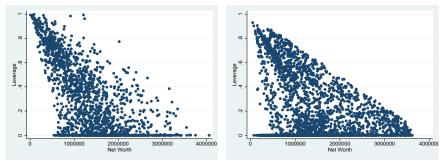
Model

Results

Conclusion

Appendix

#### Heterogeneity in Leverage Model vs. Data



(a) Data

(b) Simulation

Introduction 000000	Empirical Evidence	Model 00000000000	Results	Conclusion o	Appendix 0000		
MPC a	MPC and Leverage						

Why would leverage affect the MPC in this model?

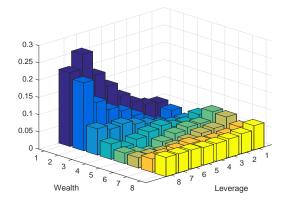
- Housing wealth is extremely liquid here:
  - Nothing prevents the household from borrowing more against its housing wealth
- But housing wealth is still somewhat illiquid: There are moving costs.
- The liquidity of housing wealth depends on proximity to the LTV-limit
  - $\Rightarrow$  Leverage measures the liquidity of housing wealth

Introduction	Empirical Evidence	Model 00000000000	Results 0000000000	Conclusion o	Appendix 0000
The Ro Model vs. D	le of Housin	g Leverage	Э		

Dep.Var:			$\Delta C_t$	
	(1) Simulation	(2) Data	(3) Simulation	(4) Data
$\Delta W_t$	0.527*** (0.042)	0.531*** (0.106)	0.203*** (0.042)	0.804*** (0.107)
$W_{t-1}$	-0.004*** (0.000)	-0.096*** (0.001)	(0.042)	(0.107)
$\Delta W_t \times W_{t-1}$	-0.000 (0.000)	0.008*** (0.001)		
$\frac{W_{t-1}}{Y_{t-1}}$	(0.000)	(0.001)	0.034***	-0.012***
			(0.000)	(0.000)
$\Delta W_t \times \frac{W_{t-1}}{Y_{t-1}}$			0.017***	-0.010***
$lev_{t-1}$	-0.091*** (0.005)	-0.337*** (0.001)	(0.000) 0.147*** (0.005)	(0.000) -0.253*** (0.001)
$\Delta W_t \times lev_{t-1}$	0.200***	0.226***	0.259***	0.206***
	(0.005)	(0.002)	(0.004)	(0.002)
Year#		X		X
$\bar{Y}$ #	X	X	X	X
CHAR#	Х	Х	Х	Х
adj. $R^2$	0.316	0.346	0.346	0.335
N	144,246	1,346,264	144,246	1,346,264

Introduction Empirical Evidence Model Results Conclusion Appendix

## MPC by Wealth and Leverage in the Model



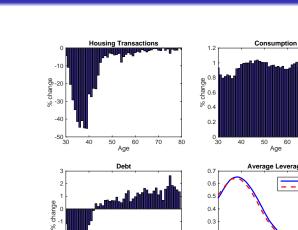
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Introduction 000000	Empirical Evidence	Model	Results 00000●00000	Conclusion o	Appendix 0000
	mplications Credit Contraction				

## • Eggertsson & Krugman (2012), Guerrieri & Lorenzoni (2011)

- Reduction in credit limit
- Constrained households are forced to reduce consumption
- No leverage
- Problem: very stylized
- Our exercise
  - A sudden change in LTV requirement
    - Geanakopoulos (2008,2011,2014)
  - Compare households' reaction with and without the policy change
  - Caveat: no general equilibrium effect

Introduction	Empirical Evidence	Model	Results oooooo●oooo	Conclusion o	Appendix 0000
	mplications Gredit Contraction				



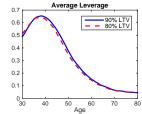
Age

0

-2

-3

-4 -30 40 50 60 70 80



60 70 80

Age

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Introduction	Empirical Evidence	<b>Model</b> 00000000000	Results ooooooo●ooo	Conclusion o	Appendix 0000
	mplications nt Tightening of Len		- Low LTV		

- A widespread narrative of the Great Recession: Shocks amplified due to high household leverage
  - Supportive Evidence: Mian, Rao and Sufi (2013), Baker (2014)
- Does this motivate tighter restrictions on lending?
  - Macroprudential policy tool: LTV-limit
    - Already implemented in New Zealand, Norway, ++
- Our exercise
  - Compare to economies that differ only by their LTV-limits
  - Steady state comparison
  - Ask: Will a lower LTV-limit reduce the marginal propensity to consume out of wealth changes?

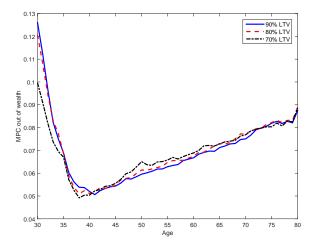
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• Wealth change of a given size

Introduction	Empirical Evidence	Model 00000000000	Results oooooooo●oo	Conclusion o	Appendix 0000
	mplications	ding Standards -	· Lower LTV		

Effect on the MDC nr and groups

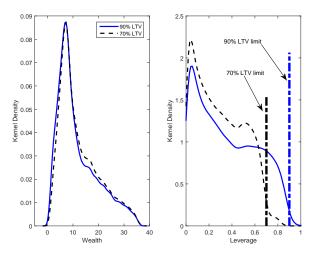
#### Effect on the MPC pr age group:



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Introduction	Empirical Evidence	Model 00000000000	Results ooooooooooooo	Conclusion o	Appendix 0000
	mplications	ding Standards -	· Lower LTV		

Distributional consequences:



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Introduction	Empirical Evidence	<b>Model</b> 00000000000	Results oooooooooo●	Conclusion o	Appendix 0000
	mplications nt Tightening of Ler	iding Standards ·	- Lower LTV		

## Upshot:

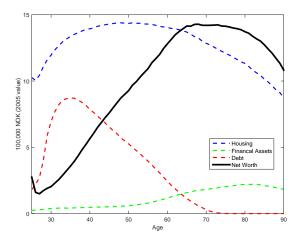
- MPC out of given wealth change largely unaffected
- Intuition: LTV tightening reduces both leverage and the leverage level that generates illiquidity.
- Interpretation: Permanent LTV-lowering is only likely reduce volatility if it reduces the magnitude of wealth shocks
  - In particular: Reduce the effect of house price changes on wealth (ignored in our study)

Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion	Appendix 0000
Conclus	ion				

- Mian-Sufi association between consumption response to wealth changes and leverage confirmed at the micro level
- A model that matches life cycle profiles of households' balance sheets implies a similar association between leverage and the MPC out of wealth as in the data
- Housing key to understanding the MPC and the role of leverage
- Down payment requirements have little effect on the MPC out of given wealth changes
  - Postpones the home ownership choice
  - To be effective, the influence must be to dampen the magnitude of wealth shocks (not in our model)

Introduction Empirical Evidence Model Results Conclusion Appendix

## Median Household Balance Sheet: Data



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Introduction	Empirical Evidence	Model	Results	Conclusion	Appendix
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Parame	ters				

#### Preferences

- a age a
- $\tilde{C}_a$  consumption index
- $p_a^S$  conditional probability of survival
- $C_a$  real non-housing consumption
- $S_a$  housing service flow
- $\alpha_a$  weight on non-housing consumption
- $\beta$  the discount factor
- $\rho$  the coefficient of relative risk aversion
- $\theta$  the elasticity of substitution
- *f<sub>a</sub>* impact of adults on non-housing consumption
- $f_c$  impact of children on non-housing consumption

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Introduction	Empirical Evidence	Model 00000000000	Results 00000000000	Conclusion O	Appendix 00●0

Income Growth and Idiosyncratic Risk

External Calibration

Residual Income Growth

$$\log Y_{ia} = f_i + Z_{ia}\beta + y_{ia}$$

Idiosyncratic risk

$$\Delta y_{ia} = \psi_{ia} + \Delta \xi_{ia}$$
$$\sigma_{\psi,a}^2 = Cov(\Delta y_{ia}, \Delta y_{ia-1} + \Delta y_{ia} + \Delta y_{ia+1})$$
$$\sigma_{\xi,a}^2 = -Cov(\Delta y_{ia}, \Delta y_{ia+1})$$

Introduction	Empirical Evidence	Model 0000000000	Results 00000000000	Conclusion O	Appendix 000
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## Initial Distribution of Net Worth, Housing, and Income

External Calibration

Group	Net Worth	Income	Housing	Homeownership
1	-16.87	3.06	15.64	0.25
2	-7.03	3.01	13.33	0.55
3	-3.44	2.33	13.33	0.36
4	-2.27	1.97	13.24	0.22
5	-1.52	2.06	13.72	0.20
6	-0.86	2.10	13.78	0.19
7	-0.27	1.99	13.76	0.17
8	0.01	1.25	14.04	0.04
9	0.24	1.99	13.92	0.16
10	1.05	2.56	14.24	0.49
11	2.66	2.82	14.45	0.83
12	4.68	2.76	15.49	0.95
13	6.78	2.57	15.70	0.98
14	8.98	2.53	16.32	0.99
15	11.27	2.32	16.83	1.00
16	13.75	2.21	18.07	1.00
17	16.56	2.09	19.70	1.00
18	20.02	2.13	22.40	1.00
19	25.73	2.12	27.71	1.00
20	51.66	2.56	43.14	0.99