

Implicit Fiscal Guarantee for Monetary Stability

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The views expressed here do not necessarily reflect the ones of Banque de France or the Eurosystem.

Motivation

Currency areas and fiscal jurisdictions

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Cryptocurrencies as decentralized payment systems

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Both arguments based on exogenously fixed actions (commitment).

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- ▶ cares about consumption: its own + people alive
- ▶ can tax the real endowment of the young (lump sum)
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- ▶ with low endowment/benevolence **autarky** is still **possible**

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1. Basic model

OLG Model: consumption-saving problem

- ▶ A representative agent born at time t maximizes:

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$$\text{young :} \quad C_{t,y} + \frac{M_t}{P_t} + S_t + T_{t,y} = W$$

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- ▶ individual endowment W , lump sum tax T ;
- ▶ agents choose consumption C and composition of savings:
- ▶ either in real cash holdings M/P
- ▶ or in freely available storage S with a return $\theta < 1$

Optimal choices of agents

- ▶ Savings:

$$D_t \equiv S_t + \frac{M_t}{P_t} = \frac{W}{2}$$

for **any** expected return (property of log-utility)

$$\rho_t = \frac{\theta S_t + M_t/P_{t+1}}{D_t}$$

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- ▶ Portfolio allocation:

$$\begin{aligned} \frac{M_t}{P_t} &= \frac{W}{2} \quad \text{and} \quad S_t = 0 && \text{if} \quad \Pi_t < \frac{1}{\theta}, \\ \frac{M_t}{P_t} + S_t &= \frac{W}{2} && \text{if} \quad \Pi_t = \frac{1}{\theta}, \\ S_t &= \frac{W}{2} \quad \text{and} \quad \frac{M_t}{P_t} = 0 && \text{if} \quad \Pi_t > \frac{1}{\theta}, \end{aligned}$$

where $\Pi_t \equiv P_{t+1}/P_t$ is the inflation rate from time t to time $t + 1$.

OLG Model: fiscal authority

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$$M_{g,t} + M_t = \bar{M}$$

with \bar{M} given (e.g. it can be shells or cryptocurrencies).

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- ▶ Look first at the no policy case: $\mathcal{P}_t = (0, 0, 0, 0)$ at any t

No policy leads to indeterminacy

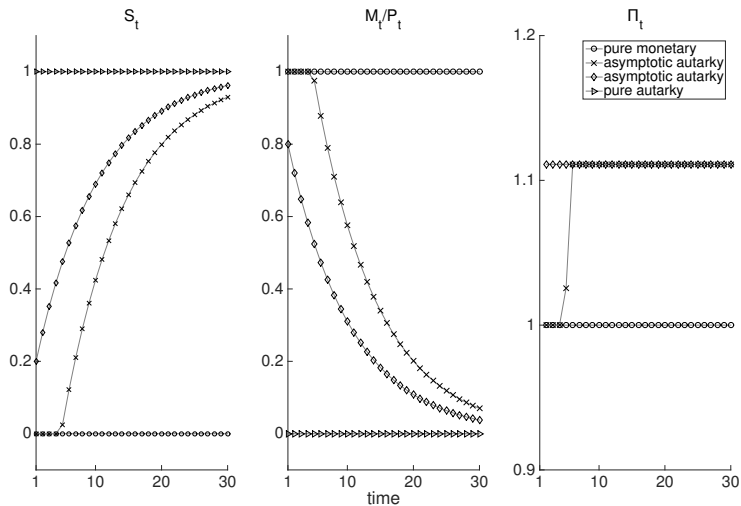


Figure: Equilibria without policy intervention for $\theta = 0.9$, $W = 2$ and $\bar{M} = 1$.

2. Optimal policy **with** state-contingent taxes

Optimal policy with state-contingent taxes

At any t , an optimal policy is a $\mathcal{P}_t^* = (T_{y,t}^*, M_{g,t}^*, G_t^*, 0)$ that solves:

$$\max_{\mathcal{P}_t, G_t} \{ \log C_{y,t} + \log C_{o,t} + \lambda \log G_t \},$$

subject to

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taking into account agents' decision process on consumption:

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and market clearing conditions, with $S_0 = 0$ and $M_0 \leq \bar{M}$.

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- ▶ no transfers to old: **optimal with heterogeneity in the absence of type-specific fiscal tools!**

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whose solution is

$$\begin{cases} G_t = \lambda C_{y,t}, & P_t = \frac{(2+\lambda)M_{t-1}}{W-(1+\lambda)\theta S_{t-1}-S_t} & \text{with } C_{y,t} \geq C_{o,t} \\ G_t = \lambda C_{y,t}, & P_t \rightarrow \infty & \text{otherwise.} \end{cases}$$

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- ▶ At some point this is unfeasible: **no asymptotic autarky!**

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- ▶ **Autarky cannot be an equilibrium!**

Optimal policy with state-contingent taxes

compare

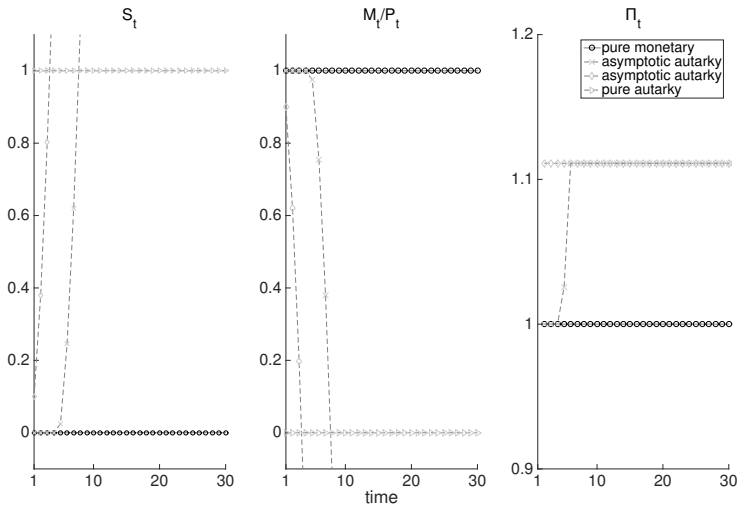


Figure: Uniqueness with optimal policy for $\theta = 0.9$, $W = 2$, $\bar{M} = 1$ and $\lambda \rightarrow 0$.

3. Optimal policy **without** state-contingent taxes

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and market clearing conditions, with $S_0 = 0$ and $M_0 \leq \bar{M}$.

Optimal policy without state-contingent taxes

At any t , an optimal policy is a $\mathcal{P}_t^* = (\bar{T}, M_{g,t}^*, G_t^*, 0)$ that solves:

$$\max_{M_{g,t}, G_t} \{ \log C_{y,t} + \log C_{o,t} + \lambda \log G_t \},$$

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- ▶ Taxes are still there but are now **fixed!**

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Optimal policy without state-contingent taxes

compare

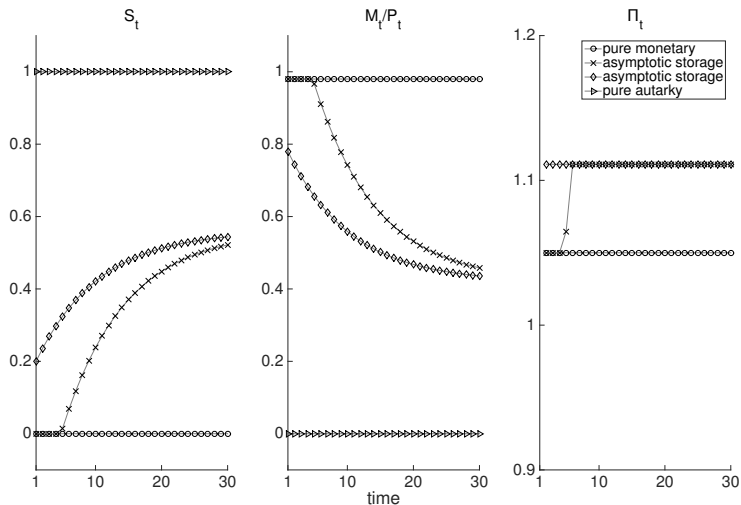


Figure: Uniqueness with fixed taxes for $\theta = 0.9$, $W = 2$, $\bar{M} = 1$ and $\lambda = 0.05$.

Multiplicity without state-contingent taxes

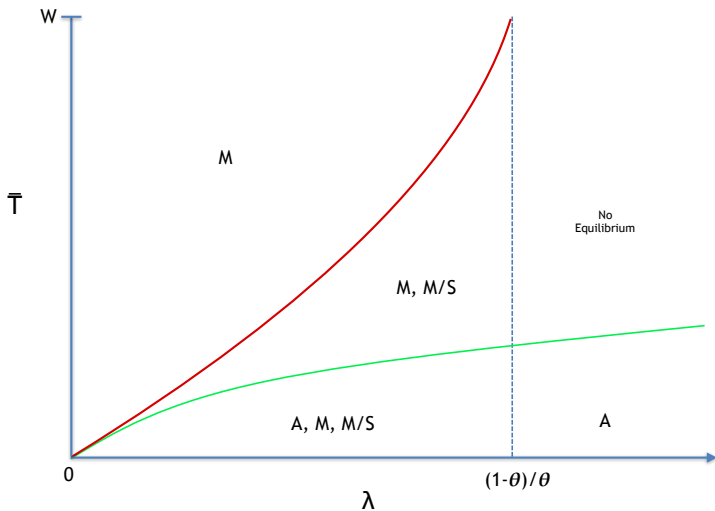


Figure: Multiplicity: A=autarky, M/S=asymptotic storage, M=pure monetary

4. Conclusion

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Money is what is guaranteed by the gov'nt...

...but also, the gov'nt will guarantee what is used as Money.

No policy leads to indeterminacy

back

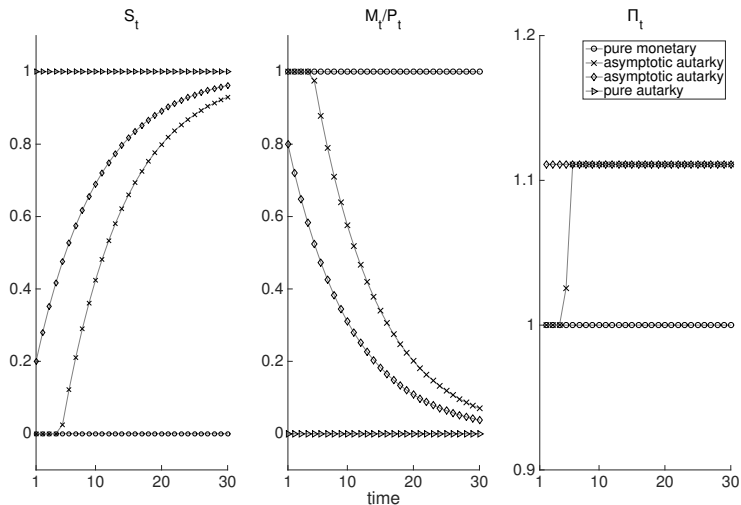


Figure: Equilibria without policy intervention for $\theta = 0.9$, $W = 2$ and $\bar{M} = 1$.

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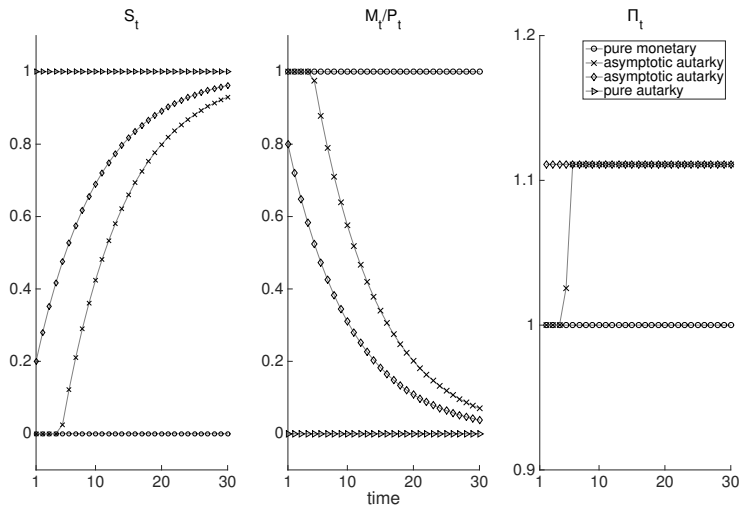


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