Falling Natural Rates, Rising Housing Volatility and the Optimal Inflation Target

Klaus Adam Oliver Pfaeuti Timo Reinelt University of Mannheim

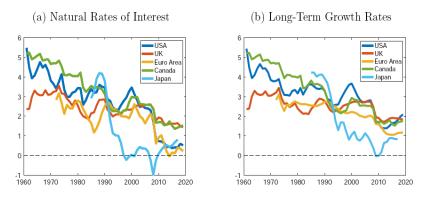
2020

- Four unfavorable macro trends in advanced economies:
 - (1) secular decline in growth rates (Summers (2014))
 - (2) secular decline in natural interest rates (Holston et al. (2017))
 - (3) upward trend in the volatility of housing prices (NEW)
 - (4) upward trend in the *volatility* of natural rates (NEW)

- Four unfavorable macro trends in advanced economies:
 - (1) secular decline in growth rates (Summers (2014))
 - (2) secular decline in natural interest rates (Holston et al. (2017))
 - (3) upward trend in the volatility of housing prices (NEW)
 - (4) upward trend in the *volatility* of natural rates (NEW)
- Common cause linking all four macro trends?

- Four unfavorable macro trends in advanced economies:
 - (1) secular decline in growth rates (Summers (2014))
 - (2) secular decline in natural interest rates (Holston et al. (2017))
 - (3) upward trend in the volatility of housing prices (NEW)
 - (4) upward trend in the *volatility* of natural rates (NEW)
- Common cause linking all four macro trends?
- Monetary policy implications of these macro trends?

Known trends: lower growth & natural rates

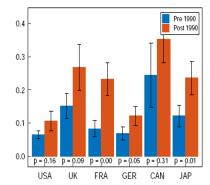


Source: Holston et al. (2017) and Fujiwara et al. (2016)

2020 3 / 45

- Macro volatility changes difficult to measure:
 - few observations
 - persistent variables, e.g., price-to-rent ratio
- Compare volatility changes over long time periods ${\sim}1960{\text{-}}1990$ versus 1990-2020

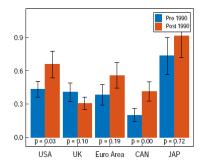
Rising Std. Deviation of the Price-to-Rent Ratio



Source: OECD database. The black lines denote the 90%-confidence bands. The *p*-values are for the null hypothesis the standard deviation has not changed pre to post 1990.

Rising Std. Deviation of the Natural Rate

Figure 2: Volatility of Natural Rates



Source: Holston et al. (2017) and Fujiwara et al. (2016) (natural rate estimates). The black lines denote the 90%-confidence bands. The reported *p*-values are for the null hypothesis that volatility has not changed from pre to post 1990.

- Present a macro model linking these trends:
 - lower growth rates => lower average natural rates
 - lower natural rates => vola of housing prices & natural rates \Uparrow
 - complicates monetary stabilization: lower bound on nominal rates

- Present a macro model linking these trends:
 - lower growth rates => lower average natural rates
 - lower natural rates => vola of housing prices & natural rates \Uparrow
 - complicates monetary stabilization: lower bound on nominal rates

Determine

- optimal MP with lower bound constraint on nominal rates

• Consider NK model with housing sector, lower bound, and subjective housing price beliefs (other beliefs rational)

- Consider NK model with housing sector, lower bound, and subjective housing price beliefs (other beliefs rational)
- Investors extrapolate (to some degree) past housing price increases (Adam, Marcet and Nicolini (JoF, 2016))

- Consider NK model with housing sector, lower bound, and subjective housing price beliefs (other beliefs rational)
- Investors extrapolate (to some degree) past housing price increases (Adam, Marcet and Nicolini (JoF, 2016))
- Extrapolative behavior in asset price & other forecasts, e.g., Adam, Marcet & Beutel (AER, 2017)
 Bordalo, Gennaioli, Ma & Shleifer (AER, forthc.)

- Consider NK model with housing sector, lower bound, and subjective housing price beliefs (other beliefs rational)
- Investors extrapolate (to some degree) past housing price increases (Adam, Marcet and Nicolini (JoF, 2016))
- Extrapolative behavior in asset price & other forecasts, e.g., Adam, Marcet & Beutel (AER, 2017)
 Bordalo, Gennaioli, Ma & Shleifer (AER, forthc.)
- Housing forecasts from Michigan HH Survey: Subjective beliefs match forecast error structure

- Consider NK model with housing sector, lower bound, and subjective housing price beliefs (other beliefs rational)
- Investors extrapolate (to some degree) past housing price increases (Adam, Marcet and Nicolini (JoF, 2016))
- Extrapolative behavior in asset price & other forecasts, e.g., Adam, Marcet & Beutel (AER, 2017)
 Bordalo, Gennaioli, Ma & Shleifer (AER, forthc.)
- Housing forecasts from Michigan HH Survey: Subjective beliefs match forecast error structure
- RE hypothesis inconsistent with Michigan forecasts

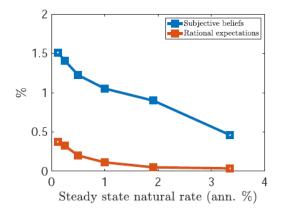
- NK model with subjective housing price beliefs: lower growth rates => lower natural rates
- Lower natural rates amplify belief-based fluctuations in housing prices

- NK model with subjective housing price beliefs: lower growth rates => lower natural rates
- Lower natural rates amplify belief-based fluctuations in housing prices
- More volatile housing price expectations
 - => more volatile (subjective) plans for non-housing consumption
 - => interest rates restoring (objectively) optimal cons. more volatile

- NK model with subjective housing price beliefs:
 lower growth rates => lower natural rates
- Lower natural rates amplify belief-based fluctuations in housing prices
- More volatile housing price expectations
 - => more volatile (subjective) plans for non-housing consumption
 - => interest rates restoring (objectively) optimal cons. more volatile
- Rational housing expectations:

No volatility increase in natural rates from lower av. natural rates

The Optimal InflationTarget



- NK model with housing & lower bound constraint
- Optimal policy problem & economic mechanisms

• Representative HH:

$$\max E_{0}^{\mathcal{P}} \sum_{t=0}^{\infty} \beta^{t} \left[\tilde{u}(C_{t};\xi_{t}) - \int_{0}^{1} \tilde{v}(H_{t}(j);\xi_{t}) dj + \tilde{\omega}(D_{t} + D_{t}^{R};\xi_{t}) \right]$$

s.t.:
$$C_{t} + B_{t} + (D_{t} - (1 - \delta)D_{t-1}) q_{t} + k_{t} + R_{t}D_{t}^{R} =$$

$$\tilde{d}(k_{t};\xi_{t})q_{t} + \int_{0}^{1} w_{t}(j)H_{t}(j)dj + \frac{B_{t-1}(1 + i_{t-1})}{\Pi_{t}} + \frac{\Sigma_{t} + T_{t}}{P_{t}}$$

 \bullet \mathcal{P} : subjective housing price beliefs, otherwise rational beliefs

- Model formulated in terms of growth-detrended variables
- Discount rate β jointly captures:
 - pure time preference rate $\widetilde{eta} \in (0,1)$
 - the steady-state growth rate g_c of marginal utility.

$$\beta \equiv \widetilde{\beta} \frac{\widetilde{u}_C(C(1+g_c))}{\widetilde{u}_C(C)},$$

- Model formulated in terms of growth-detrended variables
- Discount rate β jointly captures:
 - pure time preference rate $\widetilde{\beta}\in(\mathsf{0},\mathsf{1})$
 - the steady-state growth rate g_c of marginal utility.

$$\beta \equiv \widetilde{\beta} \frac{\widetilde{u}_C(C(1+g_c))}{\widetilde{u}_C(C)},$$

• Growth rate g_c falls => discount rate β increases

- Model formulated in terms of growth-detrended variables
- Discount rate β jointly captures:
 - pure time preference rate $\widetilde{\beta}\in(\mathsf{0},\mathsf{1})$
 - the steady-state growth rate g_c of marginal utility.

$$\beta \equiv \widetilde{\beta} \frac{\widetilde{u}_C(C(1+g_c))}{\widetilde{u}_C(C)},$$

- Growth rate g_c falls => discount rate β increases
- Decline in growth & natural rate captured via increase in eta

- Internally rational households & firms (Adam&Marcet (JET, 2011))
- HHs choose $\{C_t, H_t(j), D_t, D_t^R, k_t, B_t\}_{t=0}^{\infty}$ to maximize utility subject to the budget constraints
- Beliefs about variables beyond their control given by \mathcal{P} : { P_t , $w_t(j)$, q_t^u , R_t , i_t , Σ_t/P_t , T_t/P_t }, where

 $q_t^u \equiv q_t \tilde{u}_C(C; \xi_t)$ is housing price in marginal utility units

• Set of standard FOCs: labor-leisure choice, cons. Euler EQ

- Set of standard FOCs: labor-leisure choice, cons. Euler EQ
- 3 new optimality conditions:

Optimal housing demand : $q_t^u = \xi_t^d + \beta (1 - \delta) E_t^{\mathcal{P}} q_{t+1}^u$ Optimal housing investment: $k_t = \left(A_t^d q_t^u \frac{C_t^{\sigma^{-1}}}{C_t^{\sigma^{-1}}} \right)^{\frac{1}{1-\tilde{\alpha}}}$

Purchase vs. renting margin: $\xi_t^d = R_t \tilde{u}_C(C_t, \xi_t)$

- Supply side standard:
 - differentiated goods with Calvo price stickiness $lpha \in (0,1)$
 - Dixit-Stiglitz aggregation
- Standard firm FOCs for optimal reset price: Phillips curve
- New feature: wage/marginal costs depend on housing prices

- New Keynesian model with housing & lower bound constraint
- **②** Optimal policy problem & economic mechanisms

Nonlinear Optimal Policy Problem

$$\max_{\{Y_{t},q_{t}^{u},p_{t}^{*},w_{t}(j),P_{t},\Delta_{t},i_{t}\geq0\}} E_{0} \sum_{t=0}^{\infty} \beta^{t} U(Y_{t},\Delta_{t},q_{t}^{u};\xi_{t})$$

$$\left(\frac{p_{t}^{*}}{P_{t}}\right)^{1+\eta(\phi-1)} = \frac{E_{t}^{\mathcal{P}} \sum_{T=t}^{\infty} (\alpha)^{T-t} Q_{t,T} \frac{\eta\phi w_{T}(j)}{\eta-1} \left(\frac{Y_{T}}{A_{T}}\right)^{\phi} \left(\frac{P_{T}}{P_{t}}\right)^{\eta\phi+1}}{E_{t}^{\mathcal{P}} \sum_{T=t}^{\infty} (\alpha)^{T-t} Q_{t,T} (1-\tau_{T}) Y_{T} \left(\frac{P_{T}}{P_{t}}\right)^{\eta}$$

$$(P_{t}/P_{t-1})^{\eta-1} = (1-(1-\alpha)(p_{t}^{*}/P_{t})^{1-\eta})/\alpha$$

$$\Delta_{t} = h(\Delta_{t-1}, P_{t}/P_{t-1})$$

$$w_{t}(j) = \lambda \frac{\bar{H}_{t}^{-\nu}}{\bar{C}_{t}^{\bar{\sigma}^{-1}}} \left(\frac{Y_{t}}{A_{t}}\right)^{\phi\nu} C(Y_{t}, q_{t}^{u}, \xi_{t})^{\bar{\sigma}^{-1}} \left(\frac{p_{t}^{*}}{P_{t}}\right)^{-\eta\phi\nu}$$

$$(C(Y_{t}, q_{t}^{u}, \xi_{t}); \xi_{t}) = \lim_{T \to \infty} E_{t}^{\mathcal{P}} \left[\tilde{u}_{C}(C_{T}; \xi_{T})\beta^{T} \prod_{k=0}^{T-t} \frac{1+i_{t+k}}{P_{t+k+1}/P_{t+k}}\right]$$

$$q_{t}^{u} = \xi_{t}^{d} + \beta(1-\delta)E_{t}^{\mathcal{P}}q_{t+1}^{u}$$

Adam, Pfaeuti, Reinelt

ũc

2020 18 / 45

• Can derive insightful LQ approx. to nonlinear policy problem

• Helps understanding stabilization trade-offs for output & inflation

$$\begin{split} \max_{\{\pi_t, y_t^{gap}, i_t \geq \underline{i}\}} &- E_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{2} \left(\Lambda_{\pi} \pi_t^2 + \Lambda_y \left(y_t^{gap} \right)^2 + \Lambda_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \right) \\ \text{s.t.:} \\ \pi_t &= \beta E_t \pi_{t+1} + \kappa_y y_t^{gap} + \kappa_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) + u_t \\ y_t^{gap} &= \lim_T E_t y_T^{gap} - \varphi E_t \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ &- \frac{C_q}{C_Y} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \\ + \text{Equation(s) determining} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \end{split}$$

$$\begin{split} \max_{\{\pi_t, y_t^{gap}, i_t \geq \underline{i}\}} &- E_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{2} \left(\Lambda_{\pi} \pi_t^2 + \Lambda_y \left(y_t^{gap} \right)^2 + \Lambda_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \right) \\ \text{s.t.} \\ \pi_t &= \beta E_t \pi_{t+1} + \kappa_y y_t^{gap} + \kappa_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) + u_t \\ y_t^{gap} &= \lim_T E_t y_T^{gap} - \varphi E_t \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ &+ - \frac{C_q}{C_Y} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \\ + \text{Equation(s) determining } \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \end{split}$$

イロト イヨト イヨト イヨト

$$\begin{split} \max_{\{\pi_t, y_t^{gap}, i_t \geq \underline{i}\}} &- E_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{2} \left(\Lambda_{\pi} \pi_t^2 + \Lambda_y \left(y_t^{gap} \right)^2 + \Lambda_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \right) \\ \text{s.t.:} \\ \pi_t = &\beta E_t \pi_{t+1} + \kappa_y y_t^{gap} + \underbrace{\kappa_q}_{<0} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) + u_t \\ \underbrace{y_t^{gap}}_{t} = &\lim_T E_t y_T^{gap} - \varphi E_t \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ &- \frac{C_q}{C_Y} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \\ + &\text{Equation(s) determining} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \end{split}$$

Possibility for non-inflationary housing price booms.

Adam, Pfaeuti, Reinelt

Image: Image:

2020 22 / 45

- E > - E >

$$\begin{split} \max_{\{\pi_t, y_t^{gap}, i_t \geq \underline{i}\}} &- E_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{2} \left(\Lambda_{\pi} \pi_t^2 + \Lambda_y \left(y_t^{gap} \right)^2 + \Lambda_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \right) \\ \text{s.t.} \\ \pi_t &= \beta E_t \pi_{t+1} + \kappa_y y_t^{gap} + \kappa_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) + u_t \\ y_t^{gap} &= \lim_T E_t y_T^{gap} - \varphi E_t \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ &- \frac{C_q}{C_Y} \left(\left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \right) \\ + \text{Equation(s) determining} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \end{split}$$

• Under RE, HP fluctuations efficient:

$$\widehat{q}_t^u = \widehat{q}_t^{u*}$$

• Under RE:

Optimal policy problem same as in standard NK model (w/o housing) and ZLB

• Assumption of rational HP price expectations rejected by Michigan survey data...

- Consider Michigan Survey on HP expectations (2007-2019)
- Coibion-Gorodnichenko (AER, 2015) regressions

$$\begin{split} HP_{t+4} - E_t^{\mathcal{P}} \left[HP_{t+4} \right] &= \alpha_{CG} + \beta_{CG} \left(E_t^{\mathcal{P}} \left[HP_{t+4} \right] - E_{t-1}^{\mathcal{P}} \left[HP_{t+4} \right] \right) + \epsilon_t \end{split}$$

With RE: $\beta_{CG} = 0$

- Consider Michigan Survey on HP expectations (2007-2019)
- Coibion-Gorodnichenko (AER, 2015) regressions

$$\begin{aligned} HP_{t+4} - E_t^{\mathcal{P}} \left[HP_{t+4} \right] &= \alpha_{CG} + \beta_{CG} \left(E_t^{\mathcal{P}} \left[HP_{t+4} \right] - E_{t-1}^{\mathcal{P}} \left[HP_{t+4} \right] \right) + \epsilon_t \end{aligned}$$
With RE: $\beta_{CG} = 0$

• Adam, Marcet & Beutel (AER, 2017) regressions

$$HP_{t+4} - E_t^{\mathcal{P}} \left[HP_{t+4} \right] = \alpha_{AMB} + \beta_{AMB} HP_t + \epsilon_t$$

With RE: $\beta_{AMB} = 0$

Table: Regression Results, Michigan Survey

	2007 - 2019	2010 - 2019		
β_{CG}	2.14***	1.54***		
	(0.540)	(0.509)		
β_{AMB}	-0.36**	-0.08		
. ,	(0.147)	(0.109)		

- B - - B

• Subjective perceptions on HP growth (Adam, Marcet & Nicolini (2016))

$$q_t^u/q_{t-1}^u=b_t+\varepsilon_t,$$

 $\varepsilon_t \sim \textit{iiN}(0, \sigma_{\varepsilon}^2)$ an unobserved transitory component

 b_t is an unobserved persistent component given by

$$b_t = b_{t-1} + \nu_t,$$

with $\nu_t \sim iiN(0, \sigma_v^2)$

• With conjugate normal prior about unobserved b_t

• Subjective capital gain expectations

$$E_t^{\mathcal{P}}\left(q_{t+1}^u/q_t^u\right) = \boldsymbol{\beta}_t,$$

given by Kalman filter

$$\beta_t = \beta_{t-1} + \frac{1}{\alpha} \left(q_{t-1}^u / q_{t-2}^u - \beta_{t-1} \right)$$

 $1/\alpha$: Kalman gain

Table: Forecast errors: subj. belief model versus data

	steady-state natural rate			rate		
	2007 - 19	2010 - 19	3.34%	1.91%	1%	0.25%
β_{CG}	2.14***	1.54***	0.74	1.24	1.85	2.31
	(0.540)	(0.509)				
β_{AMB}	-0.36**	-0.08	-0.07	-0.08	-0.10	-0.15
. /	(0.147)	(0.109)				

• Equilibrium housing price

$$\begin{aligned} q_t^u &= \xi_t^d + \beta(1-\delta) E_t^{\mathcal{P}} q_{t+1}^u = \xi_t^d + \beta(1-\delta) \beta_t q_t^u \\ \implies q_t^u = \frac{\xi_t^d}{1 - \beta(1-\delta) \beta_t} \end{aligned}$$

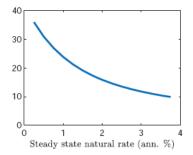
• This equation & belief updating equation determine HP dynamics

• Equilibrium housing price

$$\begin{aligned} q_t^u &= \xi_t^d + \beta (1-\delta) E_t^{\mathcal{P}} q_{t+1}^u = \xi_t^d + \beta (1-\delta) \beta_t q_t^u \\ \implies q_t^u = \frac{\xi_t^d}{1 - \beta (1-\delta) \beta_t} \end{aligned}$$

- This equation & belief updating equation determine HP dynamics
- Lower growth rates/natural rates (higher disc. factor β):
 Housing prices more sensitive to belief revisions β_t!

Figure 5: Unconditional standard deviation of housing prices q_t^u



Optimal Policy with Lower Bound Constraint

$$\begin{split} \max_{\{\pi_{t}, y_{t}^{gap}, i_{t} \geq \underline{i}\}} -E_{0} \sum_{t=0}^{\infty} \beta^{t} \frac{1}{2} \left(\Lambda_{\pi} \pi_{t}^{2} + \Lambda_{y} \left(y_{t}^{gap} \right)^{2} \right) \\ \text{s.t.} \\ \pi_{t} = \beta E_{t} \pi_{t+1} + \kappa_{y} y_{t}^{gap} + \kappa_{q} \left(\widehat{q}_{t}^{u} - \widehat{q}_{t}^{u*} \right) + u_{t} \\ y_{t}^{gap} = \lim_{T} E_{t} y_{T}^{gap} - \varphi E_{t} \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ - \frac{C_{q}}{C_{Y}} \left(\widehat{q}_{t}^{u} - \widehat{q}_{t}^{u*} \right) \\ \text{Given } \left\{ \widehat{q}_{t}^{u} - \widehat{q}_{t}^{u*} \right\}_{t=0}^{\infty} \end{split}$$

Adam, Pfaeuti, Reinelt

▶ ≣ ৩৭৫ 2020 32 / 45

イロト イヨト イヨト イヨト

Optimal Policy with Lower Bound Constraint

$$\begin{split} \max_{\{\pi_t, y_t^{gap}, i_t \geq \underline{i}\}} -E_0 \sum_{t=0}^{\infty} \beta^t \frac{1}{2} \left(\Lambda_{\pi} \pi_t^2 + \Lambda_y \left(y_t^{gap} \right)^2 \right) \\ \text{s.t.} : \\ \pi_t = \beta E_t \pi_{t+1} + \kappa_y y_t^{gap} + \kappa_q \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) + u_t \\ y_t^{gap} = \lim_T E_t y_T^{gap} - \varphi E_t \sum_{k=0}^{\infty} \left(i_{t+k} - \pi_{t+1+k} - r_{t+k}^{n,RE} \right) \\ & \underbrace{-\frac{C_q}{C_Y}}_{>0} \left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) \\ \text{Given } \left\{ \widehat{q}_t^u - \widehat{q}_t^{u*} \right\}_{t=0}^{\infty} \end{split}$$

• Volatility of housing price gap => volatility of natural rate!

Adam, Pfaeuti, Reinelt

Image: Image:

2020 33 / 45

Optimal Policy with Lower Bound Constraint

- Natural rate: real rate consistent with stable output gap
- The natural rate under subjective beliefs:

$$r_t^n \equiv r_t^{n,RE} \underbrace{-\frac{1}{\varphi} \frac{C_q}{C_Y}}_{>0} \left(\left(\widehat{q}_t^u - \widehat{q}_t^{u*} \right) - E_t \left(\widehat{q}_{t+1}^u - \widehat{q}_{t+1}^{u*} \right) \right)$$

More volatile housing prices (say due to lower average natural rate)
 => more volatile natural rate!

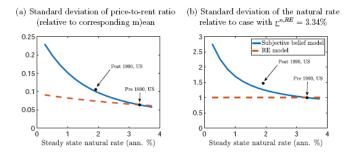
- Calibrate the model to match the pre-1990
 - (1) average natural rate
 - (2) volatility of the natural rate
 - (3) volatility of price-to-rent ratio
- Do this for the RE model and the Subj. Belief model
- What happens as natural rate falls to post-1990 average (or lower):
 - increase in the discount factor eta
 - may reflect lower steady-state growth

Parameter	Value	Source/Target		
	Preferes	nces and technology		
β	0.9917	Average U.S. natural rate pre 1990		
φ	1	Adam and Billi (2006)		
	0.057	Adam and Billi (2006)		
A _v	0.007	Adam and Billi (2006)		
κ _a	-0.0023	Adam and Woodford (2020)		
$\frac{\kappa_y}{\Lambda_{\pi}}$ $\frac{\Lambda_y}{\Lambda_{\pi}}$ $\frac{\kappa_q}{C_q}$ $\frac{C_q}{C_{\gamma}}$ s^d δ	-0.29633	Adam and Woodford (2020)		
sd	15%	Adam and Woodford (2020)		
δ	0.03/4	Adam and Woodford (2020)		
Exogenous shock processes				
ρ_{τ^n}	0.8	Adam and Billi (2006)		
σ_{r^n}	0.2940% (RE)	Adam and Billi (2006)		
	0.1394% (subj beliefs)			
ρ_{ξ^d}	0.99	Adam and Woodford (2020)		
σεα	0.0233 (RE)	Std. dev. of price-to-rent ratio pre 1990		
-	0.0165 (subj. beliefs)			
Subjective belief parameters				
α	1/0.007	Adam et al. (2016)		
β^U	1.0031	Max percent deviation of PR-ratio from mean		

▶ ≣ ৩৭৫ 2020 36/45

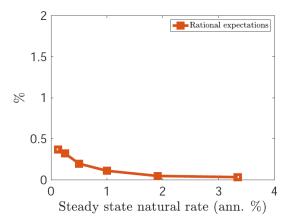
メロト メポト メヨト メヨト

Model: Non-targeted Moments



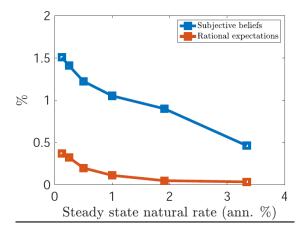
2020 37 / 45

Average Inflation under Optimal Monetary Policy



2020 38 / 45

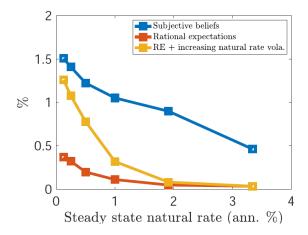
Average Inflation under Optimal Monetary Policy



2020 39 / 45

э

Average Inflation under Optimal Monetary Policy



2020 40 / 45

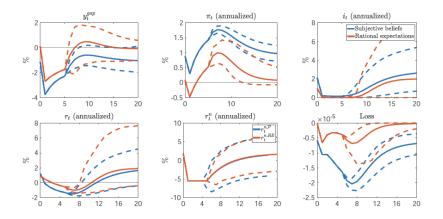
- NK model with subj. housing beliefs
 - consistent with survey evidence on housing expectations
 - lower natural rates: larger housing price & natural rate volatility
 - justify higher inflation targets due to ZLB constraint

- NK model with subj. housing beliefs
 - consistent with survey evidence on housing expectations
 - lower natural rates: larger housing price & natural rate volatility
 - justify higher inflation targets due to ZLB constraint
- Reversing unfavorable macro trends: boost long-term growth trend

Impulse Repsonse Analysis for ZLB Event

- Start economy in period 0 at ergodic mean of state variables
- 6 quarters negative natural rate that puts RE economy to ZLB & no other shocks
- After quarter 6: all shocks move gain according to their stochastic laws of motion
- Show the mean response: average over all path
- Show the 1% and 99% percentile of the response distribution
- Put the same shocks into the subjective belief model

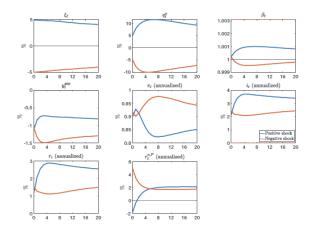
Impulse Repsonse Analysis for ZLB Event



2020 43 / 45

- < A

(Asymmetric) Leaning Against Housing Demand Shocks



2020 44 / 45

- ∢ ≣ →

Image: A math a math

Std. Deviation of the Price-to-Rent Ratio

(a) Standard Deviation of the Price-to-Rent Ratios for Different Sample Splits.

