

Real Wages and the Business Cycle in Germany

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*Workshop on Frequency Domain Research in Macroeconomics and Finance
Bank of Finland, Helsinki
20 October 2011*

Outline

- 1 Introduction
- 2 Data and stochastic properties of the series
- 3 Identification of the cyclical component
 - Linear trend
 - Beveridge-Nelson decomposition
 - Filters
 - Structural time series models
- 4 Comovements of real GDP and real wages
 - Time domain
 - Frequency domain
- 5 Conclusions

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Introduction

Relevance of an empirical analysis of the cyclical behavior of real wages

- Conflicting macroeconomic theories
 - anticyclical real wages, i.e. *Keynes (1936)*, *Barro (1990)*, *Christiano and Eichenbaum (1992)*
 - procyclical real wages, i.e. *Kydland and Prescott (1982)*, *Barro and King (1984)*
 - procyclical or acyclical real wages, i.e. *Rotemberg and Woodford (1991)*
- Identification of the sources and features of wages and labor costs dynamics
⇒ implications for monetary policy

Contribution of our study:

- The comovements between real wages and the cycle are analyzed not only in the time domain but also in the frequency domain
- Various methods are used to extract the cycle from the data in order to check the robustness of the results
- Both producer and consumer price index are used as a deflator in computing real wages
- Analysis is carried out for the whole economy
- Germany

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Data

- Quarterly data from 1970.Q1 to 2009.Q1 (157 observations)
 - real GDP
 - consumer real wages
 - producer real wages
- Seasonal adjustment with the Census–X12–ARIMA procedure
- Data prior to 1991.Q1 refer to West Germany, linked to the data of unified Germany using annual averages for 1991
- All generated data are represented in logarithms

Stochastic properties

- Testing for unit roots:
 - Augmented Dickey-Fuller test (ADF test)
 - Phillips–Perron test

⇒ underlying processes are not covariance stationary
- Testing of the first differences for unit roots
⇒ all series are generated by $I(1)$ processes

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The general framework for the trend–cycle decomposition:

$$y_t = y_t^g + y_t^c + \varepsilon_t, \quad t = 1, 2, \dots, T \quad (1)$$

y_t : natural logarithm of the considered series

y_t^g : trend

y_t^c : cycle

ε_t : irregular component

- STSM: all three components explicitly modeled
- BK filter: implicitly modeled components, extraction of the cycle through an elimination of the trend and irregular movements
- HP filter and BN decomposition: ε_t not modeled, irregular movements assigned to the cycle

Linear trend

- Quandt–Andrews test on structural breaks
 - ⇒ in all cases, the hypothesis of no structural break is rejected, estimated break points:
 - 2002.Q4 for real GDP
 - 2003.Q1 for both real wages
- Estimation of the linear broken trend model (LBT) for all three series
- Residual of the estimated model as the cyclical component uncorrelated with the trend component
- Testing of the LBT cycles for unit roots
 - ⇒ not covariance stationary, therefore excluded from further analysis

Beveridge–Nelson decomposition

- Decomposition proposed by *Beveridge and Nelson (1981)*
- The examined series are assumed to underlie an $I(1)$ process
- Trend as a prediction of future values of the series
- Trend is a random walk with drift
- Cycle is covariance stationary, correlated with trend

- **Advantages** in comparison to the linear trend model:
 - Suitable method for difference stationary processes
 - No assumptions with regard to the correlation between trend and cycle are required

- **Disadvantages:**
 - Various ARMA models can fit the data. However, this leads to various predictions and hence various trends and cycles
 - Variance of the trend can exceed variance of the series
 - Trend is a priori restricted to be a random walk

Filters

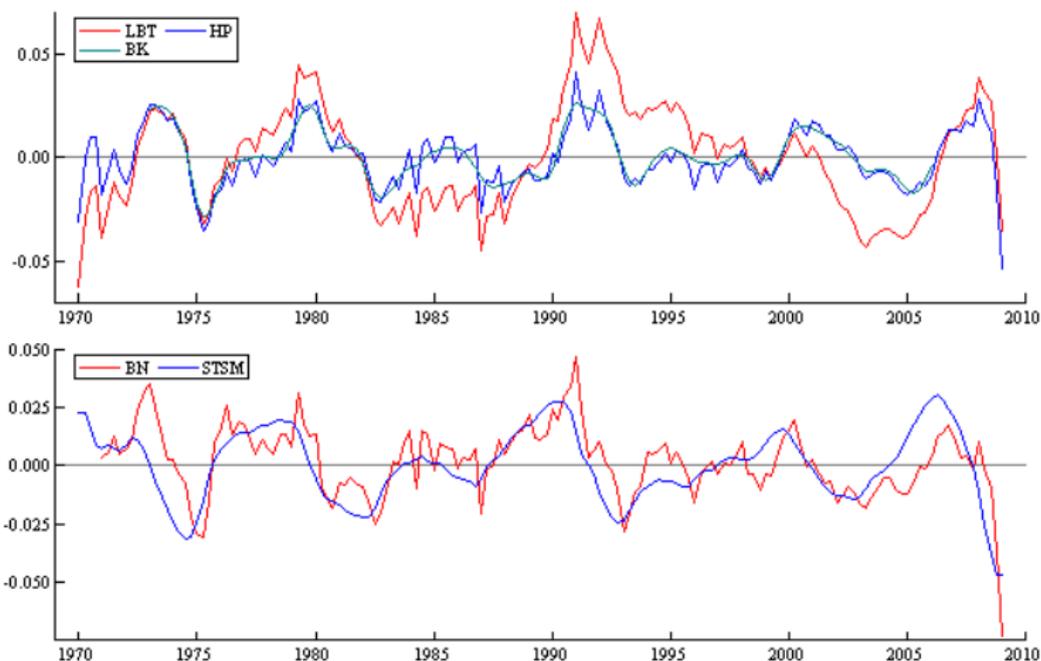
- Hodrick–Prescott (HP) filter and Baxter–King (BK) filter
- Linear filters often employed in macroeconomic applications in order to extract cycles
- HP (cyclical) filter eliminates lower “frequencies” and passes through higher “frequencies”
- BK (cyclical) filter eliminates “frequencies” outside a particular frequency band

- **Advantages:**
 - Render the data covariance stationary
 - Avoid modeling of the series
 - **Disadvantage:** it has been shown that when applied to series generated by nonstationary processes both filters induce spurious cycles
 - HP critique: e.g. *Cogley and Nason (1995)*, *Harvey and Jaeger (1993)*
 - BK critique: e.g. *Murray (2003)*
- ⇒ the results should be interpreted with some caution!

Structural time series models

- Are defined in terms of unobserved components that can, however, be directly interpreted (*Harvey, 1989*)
- **Advantages:**
 - In contrast to ad hoc filtering, they rely on stochastic properties of data
 - In contrast to ARIMA modeling, they do not aim at a parsimonious specification
- **Disadvantage:** problem of the “correct” model specification

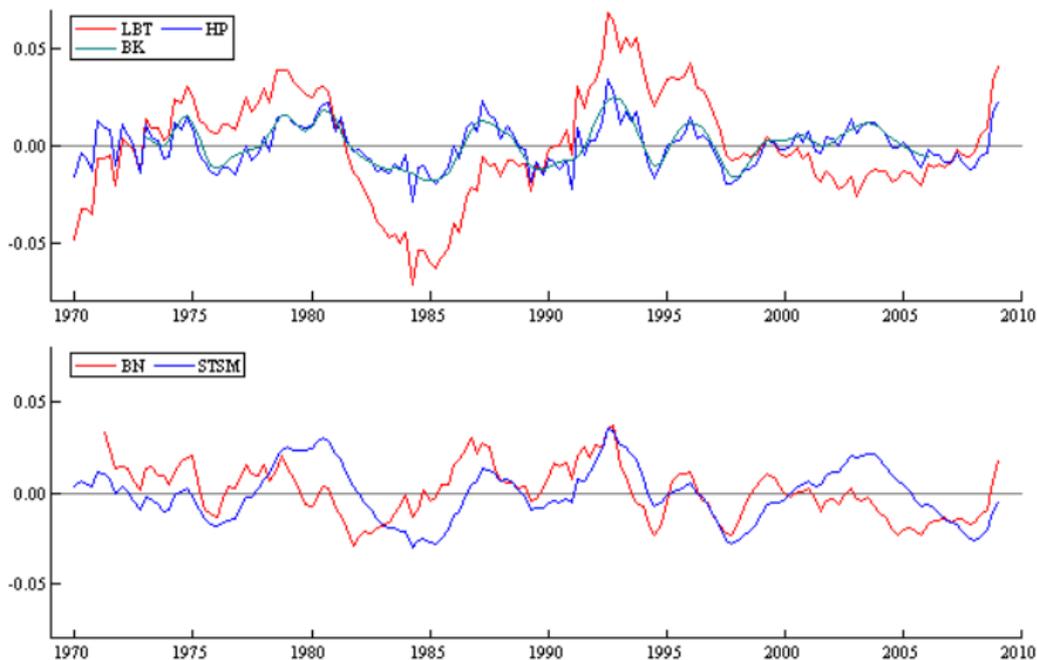
Figure: Cycles of the real GDP



LBT: Linear broken trend model
 BK: Baxter–King filter
 STSM: Structural time series model

HP: Hodrick–Prescott filter
 BN: Beveridge–Nelson decomposition

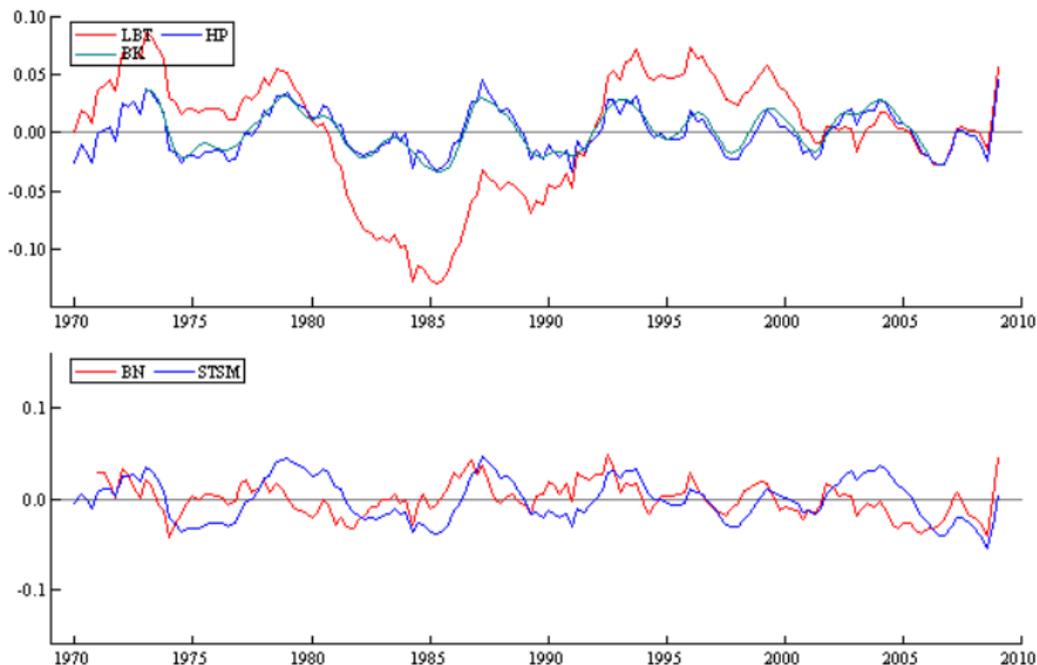
Figure: Cycles of the consumer real wage



LBT: Linear broken trend model
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Figure: Cycles of the producer real wage



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Time domain

- Traditional approach to detect the cyclical behavior
- Sample **cross–correlations** as a measure of comovements
- Real GDP cycles as a reference for the business cycle
- Analyzed bandwidth: 12 leads and 12 lags

Definitions:

- The considered real wage is **procyclical/countercyclical/acyclical** if the estimated correlation coefficients are **positive/negative/close to zero** taking into account the lead–lag structure of the series
- The considered real wage is **lagging/leading** the cycle if the largest sample cross–correlation occurs at any **lead/lag** within a given band

Results for the consumer real wage:

- The consumer real wage is procyclical and lagging the business cycle
- The strongest reaction is observed between the 5th (BN and HP cycle) and 11th quarter (STSM cycle)

Frequency domain

- Provides additional insights into the cyclicity of real wages
- **Phase angle** as the main concept adopted here
- **Phase angle** gives information about the frequency by frequency correlation and lead–lag relationship between two processes

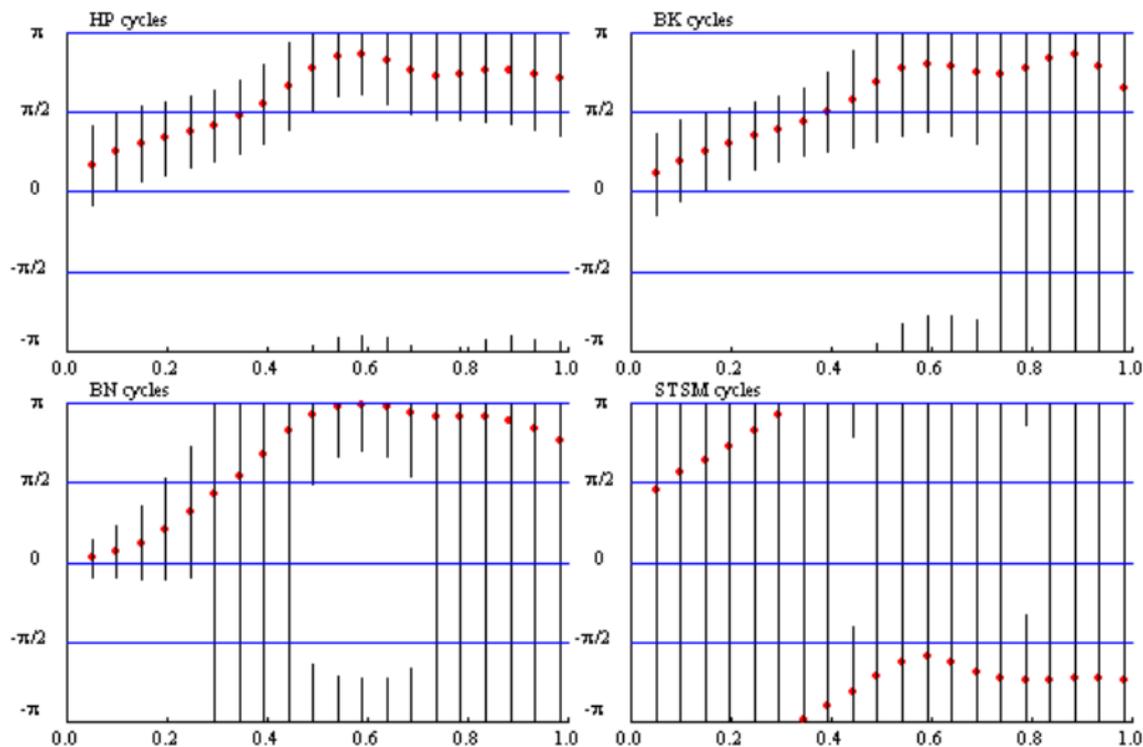
Definitions for the phase angle $\theta(\omega)$:

$\theta(\omega) > 0$ (< 0): component of real wage cycle with frequency ω **lags (leads)** the corresponding component of real GDP cycle

$|\theta(\omega)| < \pi/2$: component of real wage cycle with frequency ω is **positively** correlated with the corresponding component of real GDP cycle

$\pi/2 \leq |\theta(\omega)| \leq \pi$: component of real wage cycle with frequency ω is **negatively** correlated with the corresponding component of real GDP cycle

Figure: Phase angle: real GDP and consumer real wage cycles



Notes: The horizontal axis represents frequency ω .
 red points: point estimates, black lines: 90% confidence intervals

HP, BK, BN cycles:

- Positive values at all frequencies suggesting lagging behavior of real wage
- Statistical significant positive values rather at lower business cycle frequencies (HP, BK: up to 0.45, BN: up to 0.2)
- Values in the interval $[0, \pi/2]$ at lower frequencies (up to about 0.35) suggesting procyclical pattern of real wage
- Statistical significant procyclical pattern up to frequency 0.25

STSM cycles:

- Positive values at lower frequencies, as in the case of the HP, BK and BN cycles
- However, there are not any statistical significant values in the whole frequency range

Results for the consumer real wage:

- Procyclical and lagging behavior of longer real wage cycles
- Countercyclical and also lagging behavior of shorter real wage cycles

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Conclusions

- According to the results in the time domain, the consumer real wage displays a procyclical pattern and lags behind the business cycle though the contemporaneous correlation between the real GDP cycle and the real wage cycle is statistically insignificant
- The analysis of the phase angle in the frequency domain shows that the observed cyclicity depends on the frequency range under consideration
- At lower frequencies the consumer real wage is positively correlated with the business cycle, whereas at higher frequencies the correlation is negative
- The consumer real wage is lagging the real GDP at all frequencies
- Results for the consumer real wage are in line with nominal wage stickiness in the short run

Thank you for your attention!

Tables and figures

Table: Estimation of segmented linear trend models for real GDP and real wages

regressor	GDP	consumer wage	producer wage
	coefficients ^{a)}		
t	0.0057 (104.21)	0.0035 (59.19)	0.0052 (46.87)
$S_{k,t}$	-0.0047 (-10.49)	-0.0068 (-13.4)	-0.0112 (-11.77)
constant	5.544 (1278.237)	2.385 (510.194)	2.173 (246.321)

^{a)} t-values in parentheses. Number of observations: 157. Break point $k = 132$ for real GDP and $k = 133$ for real wages.

Here: the assumed general model as in eq. (1) with

- $\varepsilon_t \sim \mathcal{NID}(0, \sigma_\varepsilon^2)$
- y_t^g as defined in *Koopman et al. (2009)*
- y_t^c as suggested in *Koopman et al. (2009)*, *Koopman et al. (2008)*, *Harvey and Streibel (1998)*

Model for the stochastic trend component y_t^g :

$$\begin{aligned} y_{t+1}^g &= y_t^g + \beta_t + \eta_t, & \eta_t &\sim \mathcal{NID}(0, \sigma_\eta^2) \\ \Delta^m \beta_{t+1} + \zeta_t &= (1 - L)^m \beta_{t+1} + \zeta_t, & \zeta_t &\sim \mathcal{NID}(0, \sigma_\zeta^2) \end{aligned} \quad (2)$$

β_t : slope of the trend

m : order of the slope ($m = 1, 2, 3, \dots$)

Model for the cycle y_t^c :

$$\begin{bmatrix} y_{t+1}^c \\ y_{t+1}^{c*} \end{bmatrix} = \rho \begin{bmatrix} \cos(\omega) & \sin(\omega) \\ -\sin(\omega) & \cos(\omega) \end{bmatrix} \begin{bmatrix} y_t^c \\ y_t^{c*} \end{bmatrix} + \begin{bmatrix} \chi_t \\ \chi_t^* \end{bmatrix}, \quad (3)$$

$$\begin{bmatrix} \chi_t \\ \chi_t^* \end{bmatrix} \sim \mathcal{NID}(\mathbf{0}, \sigma_\chi^2 \mathbf{I}_2),$$

y_t^{c*} : auxiliary variable

ω : frequency ($0 \leq \omega \leq \pi$)

ρ : damping factor ($0 \leq \rho \leq 1$)

- Starting point for all three series:
 - no variance restrictions
 - $m = 1$ local linear trend
 - Results of the specification:
 - real GDP: $\sigma_{\eta}^2 = 0, m = 1$
 - real wage: $\sigma_{\eta}^2 = 0, m = 2$
 - Diagnostic checking:
 - Ljung–Box autocorrelation test
 - Goldfeld–Quandt heteroscedasticity test
 - Bowman–Shenton normality test
- ⇒ the models are correctly specified

Table: Contemporaneous and largest sample cross-correlations between the real GDP cycle and the particular real wage cycle by various decomposition methods

GDP with	methods			
	BN	HP	BK	STSM
consumer real wage	0,1169 0,4879*(+6)	0,0124 0,4572*(+6)	0,1438 0,6346*(+5)	-0,1677* 0,4099*(+11)
producer real wage	0,0279 0,2718*(+6)	-0,0423 0,2381*(+7)	0,0314 0,315*(+7)	-0,0362 0,2163*(+10)

Notes: " * " indicates statistical significance at the 5% level

Findings for the consumer real wage:

- Except for the STSM cycle, the estimates of the contemporaneous cross-correlations are statistically insignificant at the 5% level
- Low practical significance, most apparent in the case of the HP cycle
- Leads of the real wage cycles: sample cross-correlations become significant and are positive (STSM cycle: not until the 6th lead)
- Lags of the real wage cycles: almost all sample cross-correlations are statistically insignificant in the case of the HP, BK and BN cycles

Producer real wage:

- All estimated contemporaneous cross-correlations are statistically insignificant at the 5% level
- Leads of the real wage cycles: similar pattern as in the case of the consumer real wage, but the sample cross-correlations are not as high
- Lags of the real wage cycles: almost all sample cross-correlations are statistically insignificant

⇒ summing-up:

- procyclical and lagging the cycle
- the strongest reaction observed between the 6th (BN cycle) and 10th quarter (STSM cycle)

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⇒ summing-up:

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Figure: Data in logarithms

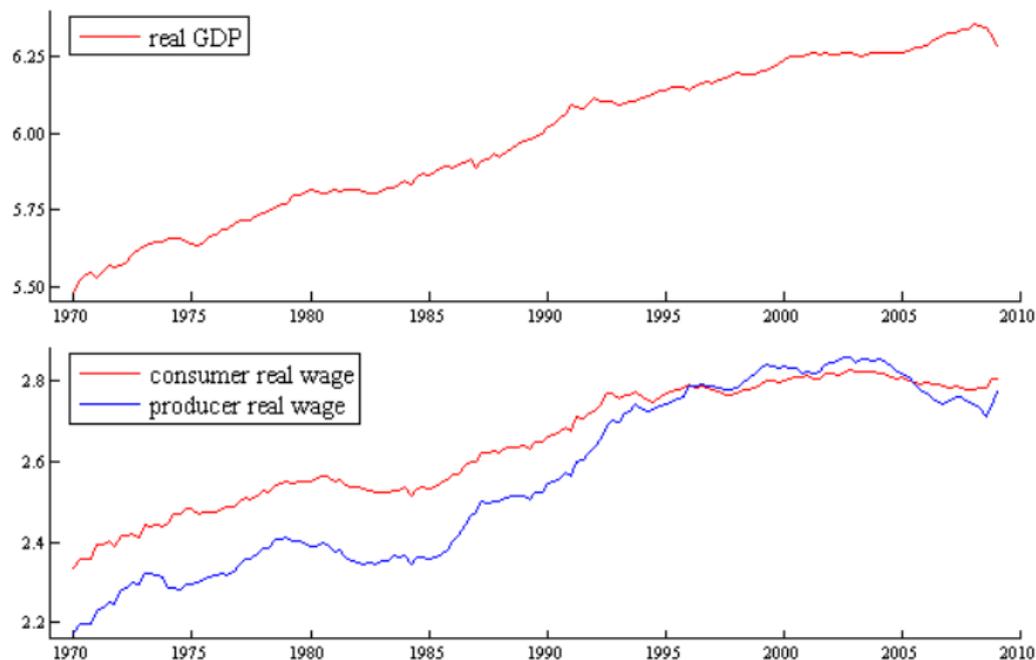
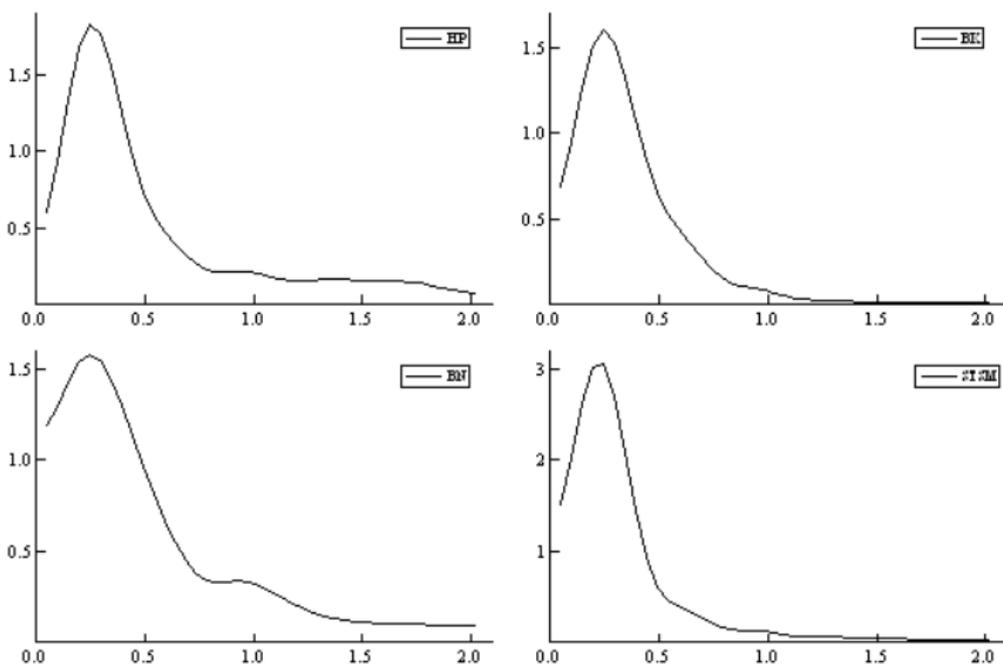


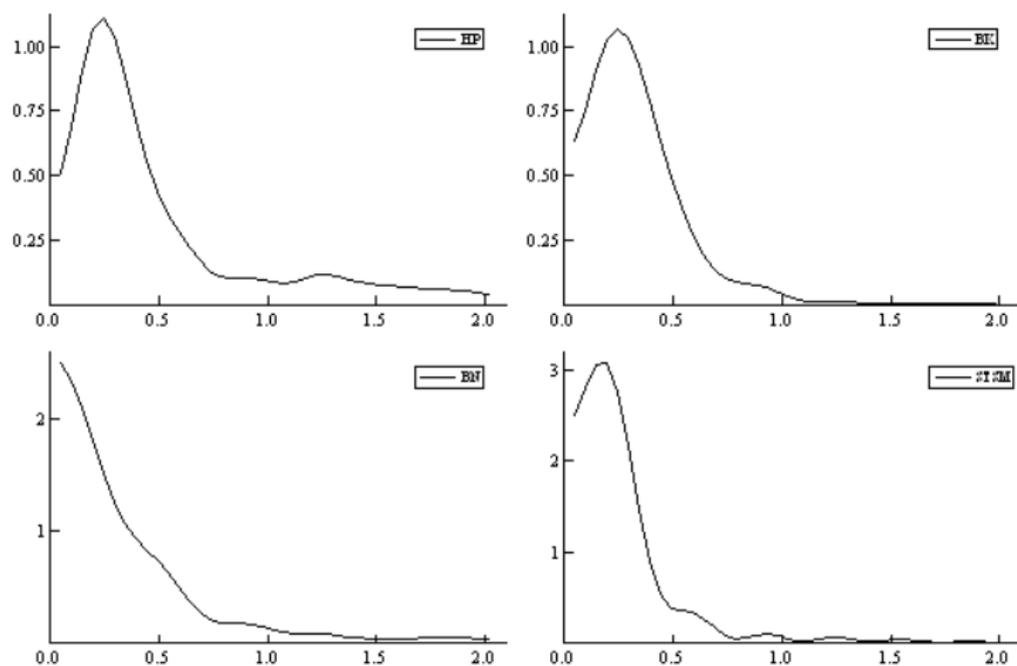
Figure: Spectra of the real GDP cycles



Notes: The horizontal axis represents frequency ω .

The values on the vertical axis have been multiplied by 10^4 .

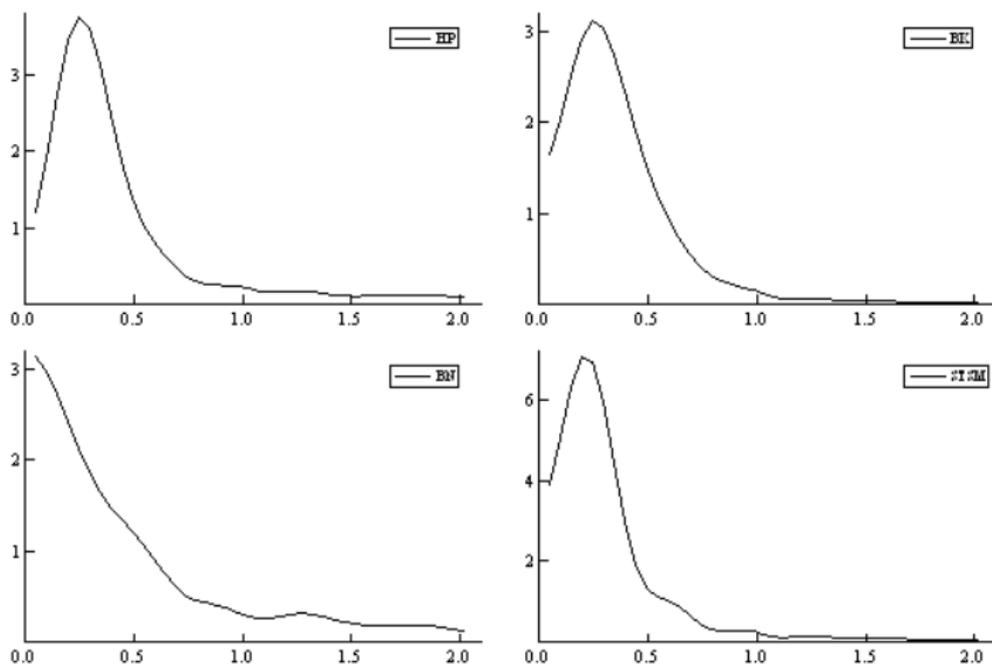
Figure: Spectra of the consumer real wage cycles



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Figure: Spectra of the producer real wage cycles

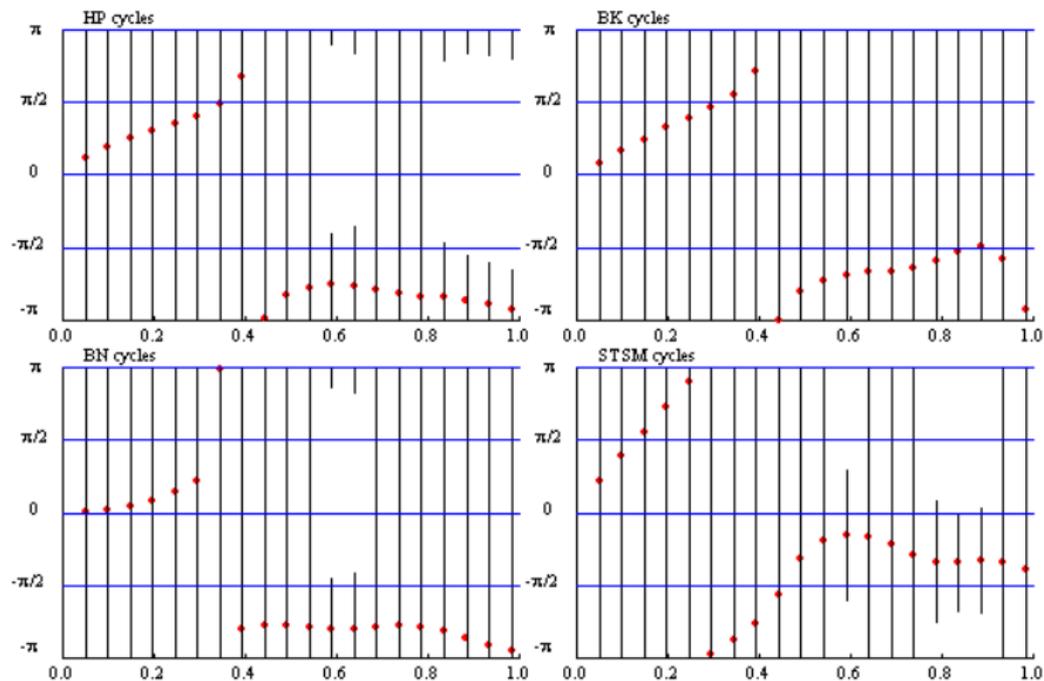


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Producer real wage

Figure: Phase angle: real GDP and producer real wage cycles



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 red points: point estimates, black lines: 90% confidence intervals

Modifications and new results

- 1 **Initial general model for the stochastic trend component y_t^g :**

$$\begin{aligned} y_{t+1}^g &= y_t^g + \beta_t + \eta_t, & \eta_t &\sim \mathcal{NID}(0, \sigma_\eta^2) \\ \beta_{t+1} &= \beta_t + \zeta_t, & \zeta_t &\sim \mathcal{NID}(0, \sigma_\zeta^2), \end{aligned} \quad (4)$$

- 2 The initial specification seems to be inappropriate for the real wages
- 3 Low variances of the cycle components with at the same time high variances of the irregular components as an indicator of possibly omitted informations
- 4 Hartz reforms starting from January 1, 2003 as an event with a great impact on the German labor market
- 5 Initial model extended by a slope intervention variable from 2003.Q1 on to take account of the additional information

Model for the cycle y_t^c :

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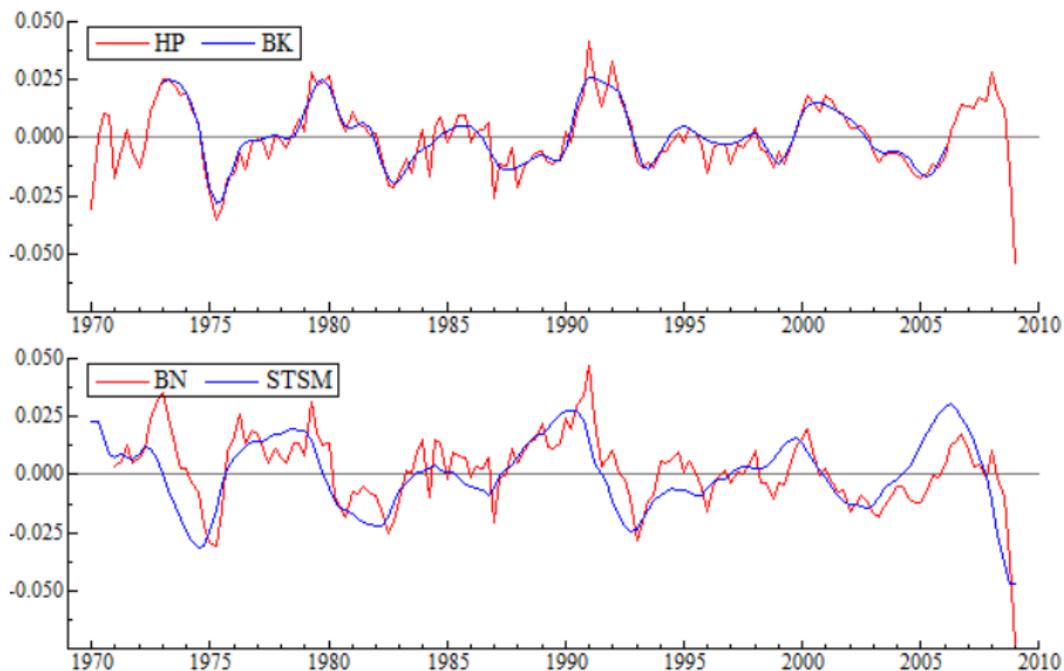
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Figure: Cycles of the real GDP



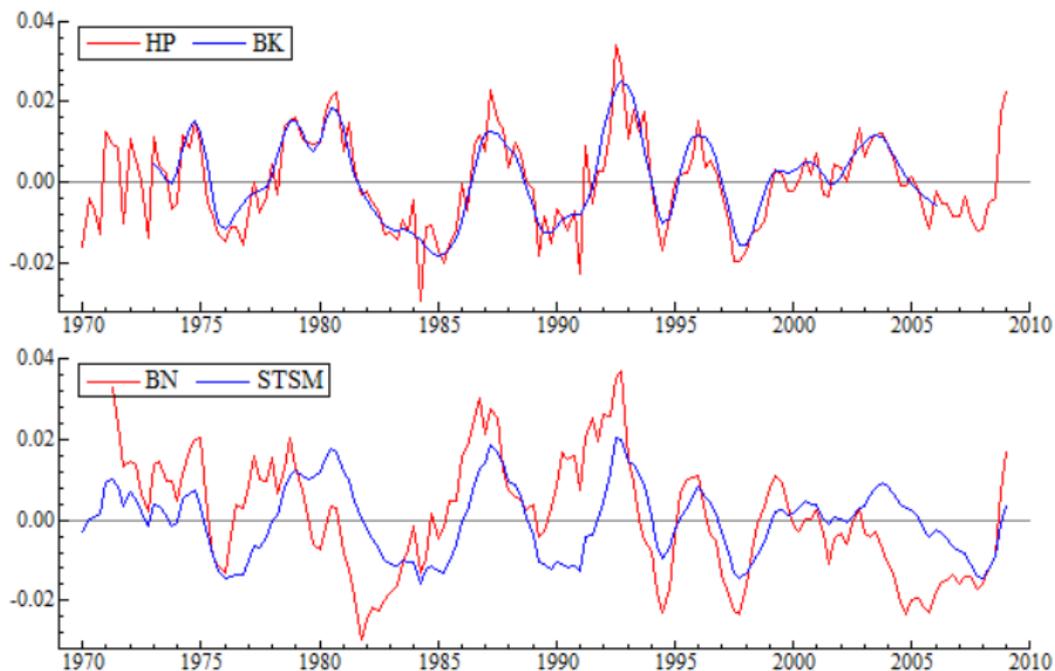
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BK: Baxter–King filter

BN: Beveridge–Nelson decomposition

STSM: Structural time series model

Figure: Cycles of the consumer real wage



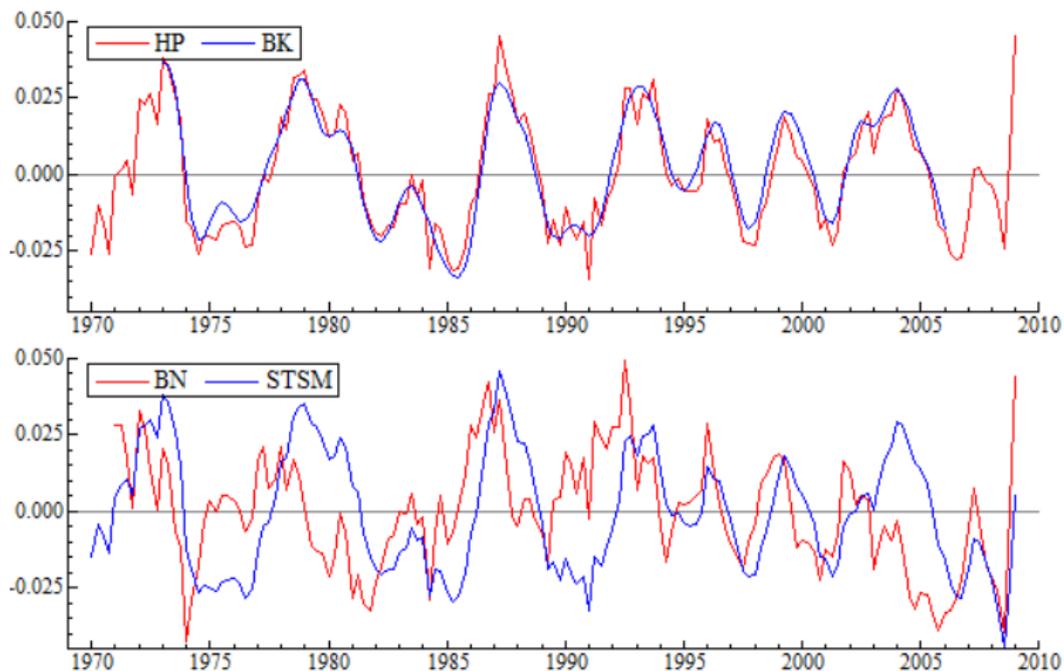
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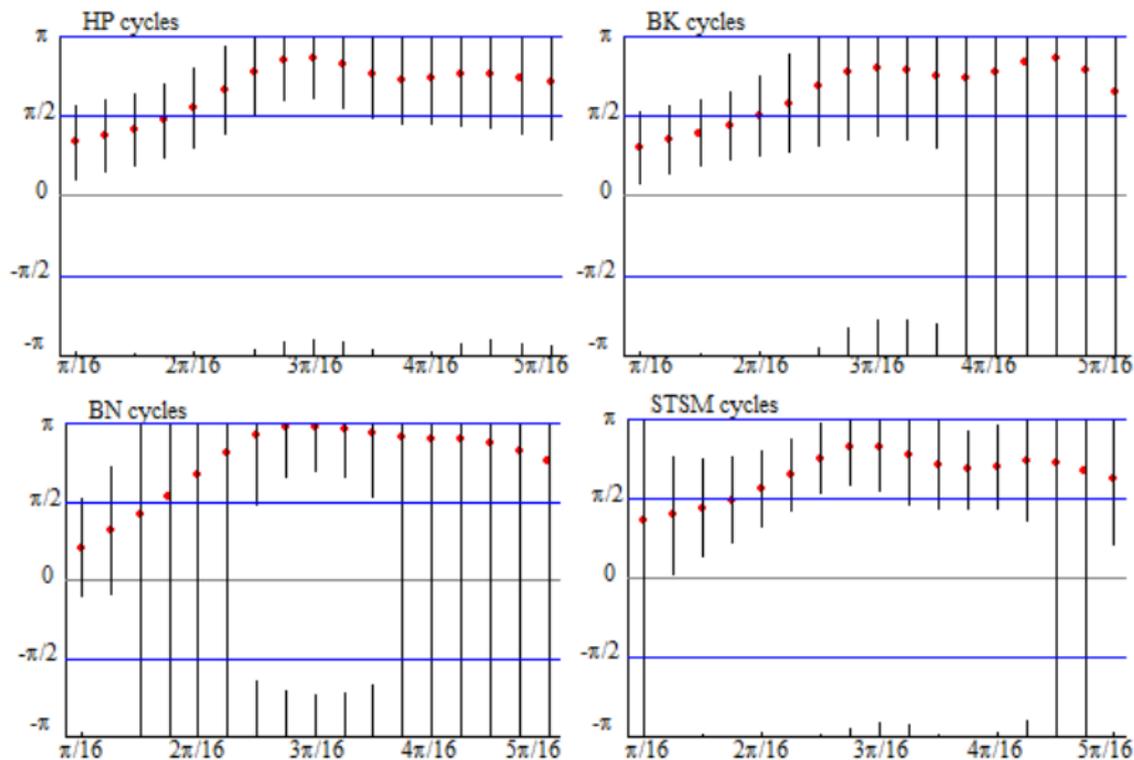
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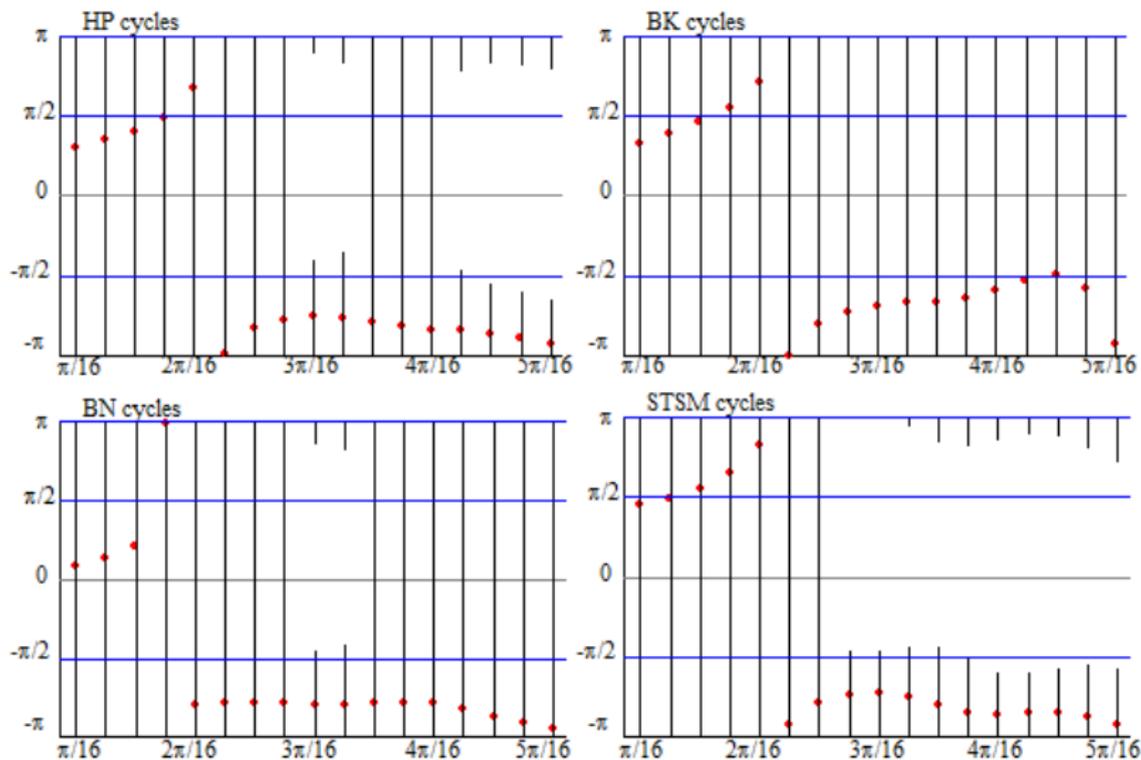
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Figure: Phase angle: real GDP and consumer real wage cycles



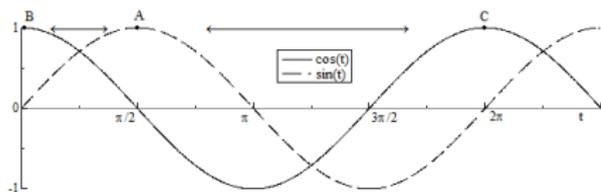
Notes: The horizontal axis represents the (angular) frequency ω .

Figure: Phase angle: real GDP and producer real wage cycles

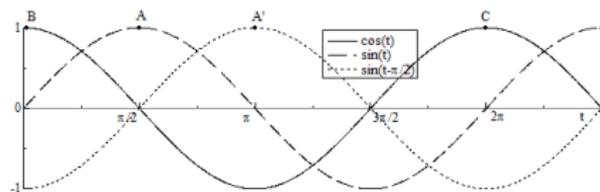


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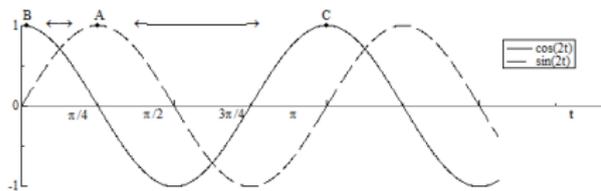
Figure: Examples of phase shifts between cyclical components



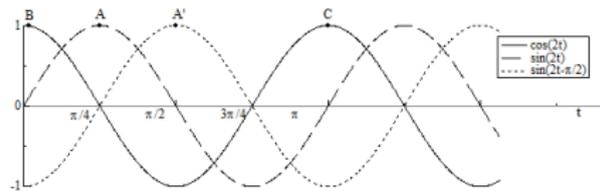
(a)



(b)



(c)



(d)