Monetary policy and endogenous financial crises

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- Loose monetary policy can help to stave off financial crises (e.g. 9/11 terrorist attacks, Covid–19),
- ... but low-for-long rates can also induce search-for-yield and be a cause of financial imbalances/instability (e.g. Great Financial Crisis, Silicon Valley Bank)

- 1. What are the channels through which monetary policy (MP) affects financial stability (FS)?
- 2. Should monetary policy deviate from price stability to promote financial stability?
- 3. To what extent may MP itself brew financial vulnerabilities?
 - \rightarrow Needed: models where MP affects the incidence and severity of crises

- Textbook New Keynesian (NK) model, with capital accumulation and sticky prices
 - + Idiosyncratic productivity shocks \rightarrow capital reallocation among firms via a credit market
 - + Financial frictions \rightarrow credit market prone to endogenous collapse when borrowers search for yield
 - + Global solution \rightarrow capture nonlinearities and dynamics far away from steady state
- MP is the "only game in town" (*e.g.* no macroprudential policy)

Contribution to the literature

- 1. MP affects FS both in the *short run* via aggregate demand and in the *medium run* via capital accumulation
- 2. By deviating from strict inflation targeting (SIT), and reacting to output and financial fragility alongside inflation, the central bank can improve both FS and welfare
- 3. MP can lead to a crisis if the policy rate remains too low for too long and then increases abruptly

- 1. Extended New-Keynesian model
- 2. Anatomy of financial crises
- 3. "Divine Coincidence" revisited
- 4. Monetary policy discretion as a source of financial instability

Extended New-Keynesian model

- Central bank: sets nominal interest rate Monetary Policy Rules
- Household: representative, works, consumes, saves (nominal bonds, firm equity) Optimisation problem
- Retailers: monopolistic, diversify intermediate goods, sticky prices Optimisation problem
- Intermediate goods firms: competitive, issue equity, invest, produce with labor and capital
 - + Idiosyncratic productivity shocks \rightarrow capital reallocation among firms via a credit market

- Continuum of 1-period firms indexed by $j \in [0,1]$
- End of t 1: Firms are similar and <u>all</u> get start-up equity funding P_{t-1}Q_{t-1} and purchase capital K_t = Q_{t-1}

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- **Beginning of** *t*: firm *j* has access to a production technology

$$Y_t(j) = A_t(\omega_t(j) \mathcal{K}_t(j))^{\alpha} \mathcal{N}_t(j)^{1-\alpha}, \quad \text{where } \omega_t(j) = \begin{cases} 0 & \text{with probability } \mu \to \text{Unproductive} \\ 1 & \text{with probability } 1-\mu \to \text{Productive} \end{cases}$$

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• Upon observing $\omega_t(j)$, firm j may adjust its capital from K_t to $K_t(j)$ via a credit market

<u>No credit frictions</u>: \Rightarrow same equilibrium as in the textbook NK model with a representative firm

- Asymmetric Information: $\omega_t(j)$ is private information
- Limited Commitment: firm *j* may borrow, purchase capital goods, and abscond with them in search for yield

 $\Rightarrow\,$ Borrowing limit is the same for all firms, and credit market is fragile



Incentive Compatibility Constraint:

An unproductive firm has two options:

- 1. Behave: sell its capital to lend the proceeds at equilibrium loan rate $r_t^c \rightarrow (1 + r_t^c)K_t$
- 2. **Misbehave:** borrow to buy more capital $K_t^p K_t$ (*i.e.* mimic productive), abscond $\rightarrow (1 \delta)K_t^p \theta(K_t^p K_t)$

• Incentive Compatibility Constraint:

Unproductive firms lend *iff* the equilibrium loan rate r_t^c is high enough

$$\rightarrow \begin{cases} (1+r_t^c)K_t \ge (1-\delta)K_t^p - \theta(K_t^p - K_t) \\ \text{where } r_t^c \text{ satisfies } \mu K_t = (1-\mu)(K_t^p - K_t) \end{cases} \Leftrightarrow r_t^c \ge \overline{r}^k \equiv \frac{(1-\theta)\mu - \delta}{1-\mu} \end{cases}$$

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• Participation Constraint:

Productive firms borrow iff r_t^c is lower than their return on capital r_t^k

$$r_t^c \leqslant r_t^k \equiv \frac{p_t}{P_t} \frac{\alpha Y_t^p}{K_t^p} - \delta = \frac{p_t}{P_t} \frac{\alpha Y_t}{K_t} - \delta$$

Credit market equilibrium

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• Trade is possible iff the marginal return on capital $r_t^k \geq \overline{r}^k$

Normal times: when r^k_t ≥ 7^k and firms trade on the credit market, r^c_t = r^k_t ≥ 7^k, capital is fully reallocated, aggregate production function is as in the credit-frictionless economy

$$Y_t = A_t K_t^{\alpha} N_t^{1-\alpha}$$

 Crisis times: when r^k_t < r^k and firms don't trade on credit market, capital is not reallocated, unproductive firms keep capital idle and capital mis-allocation lowers TFP

$$Y_t = A_t \left((1 - \mu) K_t \right)^{\alpha} N_t^{1 - \alpha}$$

MP affects financial fragility in the short and medium run

Condition for a crisis

$$\frac{\alpha Y_t}{\mathcal{M}_t \mathcal{K}_t} \leqslant (1-\tau) \left[\frac{(1-\theta)\mu - \delta}{1-\mu} + \delta \right]$$



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• Short-run: through macro-economic stabilization \rightarrow Y- and \mathcal{M} -channels



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- Short-run: through macro–economic stabilization \rightarrow Y– and \mathcal{M} –channels
- Medium-run: through capital accumulation → K–channel

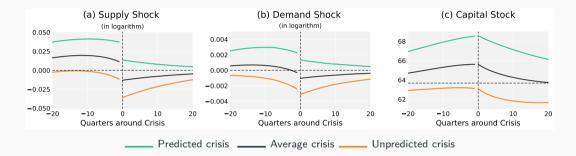
Two types of polar crises

Anatomy of financial crises

- Quarterly parametrization. Only two non-standard parameters
 - 1. μ : share of unproductive firms set to 5% to have a productivity fall by 1.8% due to financial frictions during a crisis
 - 2. θ : default cost set to 0.52 to have the economy spend 10% of the time in crisis (under TR93)
- Global solution and simulation of the (nonlinear) model over ten million periods
- The analysis focuses on the dynamics around financial crises and on crisis statistics



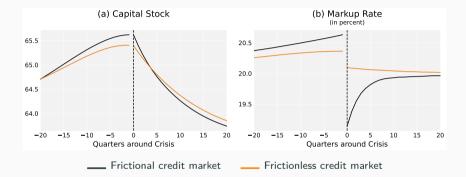
Average crisis dynamics and crisis variety under the Taylor Rule



→ Some crises break out on the back of an investment boom, others follow severe adverse non-financial shocks

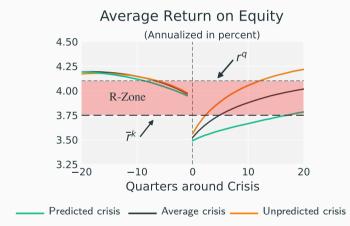


"Precautionary savings" and "markup" externalities



- The household accumulates precautionary savings in anticipation of revenue losses
- Retailers frontload price increases in anticipation of inflationary pressures
- \Rightarrow Individual "hedging" behaviors precipitate the crisis via K– and M–channels

The "yield gap" $(1 + r_t^q)/(1 + r^q)$ as index of financial fragility



"Divine Coincidence" revisited

The price-financial stability trade-off

- Under SIT, the economy spends 9.4% in a crisis and prices are fully stable.
- Reducing the incidence of crises below 9.4% necessarily entails deviating from price stability

		Rule		Mo	odel with F	inancial Fric	tions		
	pa ϕ_{π}	ramete ϕ_y	rs ϕ_r	Time in Crisis/Stress (in %)	Length (quarters)	Output Loss (in %)	$\operatorname{Std}(\pi_t)$ (in pp)	Welfare Loss (in %)	
					SIT				
(6)	$+\infty$	-	-	9.4	5.1	8.1	0	0.23	



- Under SIT, the economy spends 9.4% in a crisis and prices are fully stable.
- Reducing the incidence of crises below 9.4% necessarily entails deviating from price stability
- E.g.: when the central bank reacts to output, financial fragility and inflation, the incidence of crises can be lowered to 5.4%, but inflation volatility rises to 1.16 pp (in standard deviations)

	Rule			Model with Financial Frictions						
	р	arameter	S	Time in	in Length Output		$Std(\pi_t)$	Welfare		
	ϕ_{π}	ϕ_y	ϕ_r	Crisis/Stress (in %)	(quarters)	Loss (in %)	(in pp)	Loss (in %)		
					SIT					
(6)	$+\infty$	-	-	9.4	5.1	8.1	0	0.23		
	Augmented Taylor-type Rules									
(7)	1.5	0.125	5.0	5.4	3.9	5.5	1.16	0.65		



Deviating from price stability can improve welfare

- E.g.: Reacting to output and financial fragility alongside inflation can improve welfare upon SIT

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(6)	$+\infty$	-	-	9.4	5.1	8.1		0.23	
				Augmented	Taylor-ty	pe Rules			
(9)	5.0	0.125	25.0	6.9	4.7	6.6	0.19	0.18	
(10)	10.0	0.125	75.0	6.3	4.6	6.4	0.09	0.16	

- "Backstop policy rule": state-contingent rule whereby the central bank commits to deviate from its standard rule (e.g. SIT, Taylor rule) in the face of financial stress so as to avoid a crisis
- Under SIT-backstop, welfare gains relative to SIT are larger than under Augmented Taylor-type Rules

	Rule parameters $\phi_{\pi} \qquad \phi_{\nu} \qquad \phi_{r}$			Model with Financial Frictions					
				Time in Crisis/Stress (in %)	Length (quarters)	Output Loss (in %)	$\operatorname{Std}(\pi_t)$ (in pp)	Welfare Loss (in %)	
	φ_{π}	ϕ_y	ϕ_r		(quarters)	LO35 (III /0)	(11 pp)	LOSS (III 70)	
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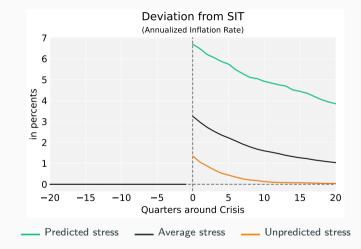
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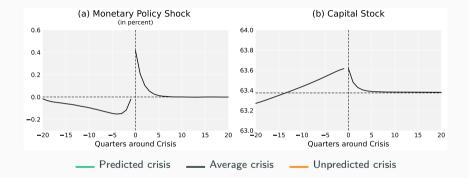
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Crises are avoided under "backstop rules" with exceptionally loose policy



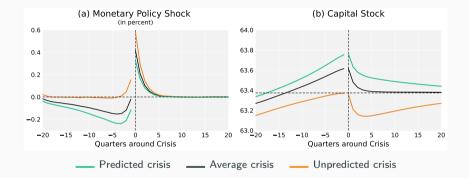
Monetary policy discretion as a source of financial instability

Discretionarily keeping rates too low for too long may lead to a crisis



- Discretionary deviations from TR93 ightarrow simulate the model with MP shocks only
- Crises occur after a "Great Deviation"...(Taylor (2011)) Deviations from Taylor rule
- ... when the central bank abruptly reverses its policy stance Evidence Schularick et al (2021)

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Takeaways

- NK model with micro-founded endogenous crises where MP affects FS via Y-M-K channels:
- Several novel policy insights:
 - → Systematic response to output and yield gap (\neq SIT) improves both FS and welfare
 - \rightarrow Backstop policy is effective and normalisation path depends on the nature of the stress
 - → "Low-for-long" policy followed by abrupt hike may lead to crisis

APPENDIX

- We study how MP affects FS in a NK model with endogenous microfounded crises
- Monetary policy and financial stability (reduced form models of endogenous crises) Woodford (2012), Filardo and Rungcharoentkitkul (2016), Svensson (2017), Gourio, Kashyap, Sim (2018), Ajello, Laubach, Lopez–Salido, Nakata (2019), Cairo and Sim (2018), Borio, Disyatat and Rungcharoentkitkul (2019)
- Micro-founded models of endogenous financial crises
 Boissay, Collard, Smets (2016), Benigno and Fornaro (2018), Gertler, Kiyotaki, Prestipino (2019), Paul (2020)
- Our approach: fragility of financial markets (≠ institutions) and search-for-yield behaviours (≠ collateral constraints)



• Sets nominal interest rate *i*_t on risk-free public bond *B*_t according to a Taylor-type policy rule:

$$1+i_t=rac{1}{eta}(1+\pi_t)^{\phi_\pi}\left(rac{Y_t}{ar{Y}}
ight)^{\phi_\pi}$$

• We also experiment with alternative rules including financially-augmented Taylor rules and SIT



Households

The representative household consumes a basket of goods C_t, works N_t, invests in a private nominal bond B_t in zero net supply and in intermediate goods firm j ∈ [0, 1]'s equity Q_t(j)

$$\max_{C_t, N_t, B_t, Q_t(j)} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{C_t^{1-\sigma}}{1-\sigma} - \chi \frac{N_t^{1+\varphi}}{1+\varphi} \right]$$

s.t.
$$\int_{0}^{1} P_{t}(i)C_{t}(i)di + B_{t} + P_{t} \int_{0}^{1} Q_{t}(j)dj \leq W_{t}N_{t} + (1+i_{t-1}^{b})B_{t-1} + P_{t} \int_{0}^{1} (1+r_{t}^{q}(j))Q_{t-1}(j)dj + \Upsilon_{t}$$
where
$$i_{t}^{b} \equiv \frac{1+i_{t}}{Z_{t}} - 1$$

is the private bond yield, with Z_t the wedge between the private yield and the policy rate i_t

• Z_t acts as an aggregate demand shock

Households' optimality conditions:

$$\begin{split} \frac{\chi N_t^{\sigma}}{C_t^{-\sigma}} &= \frac{W_t}{P_t} \\ 1 &= \beta (1+i_t^b) \mathbb{E}_t \left[\left(\frac{C_{t+1}}{C_t} \right)^{-\sigma} \frac{1}{1+\pi_{t+1}} \right] \\ 1 &= \beta \mathbb{E}_t \left[\left(\frac{C_{t+1}}{C_t} \right)^{-\sigma} \left(1+r_{t+1}^q(j) \right) \right] \quad \forall j \in [0,1] \\ Q_t(j) &= Q_t \quad \forall j \in [0,1] \end{split}$$

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Retailers

where

 Monopolistic retailer i ∈ [0, 1] produces a differentiated final good using intermediate goods and sets its price subject to quadratic adjustment costs à la Rotemberg (1982):

$$\max_{P_t(i), Y_t(i)} \mathbb{E}_0 \sum_{t=0}^{\infty} \Lambda_{0,t} \left[\frac{P_t(i)}{P_t} Y_t(i) - \frac{(1-\tau)p_t}{P_t} Y_t(i) - \frac{\varsigma}{2} \left(\frac{P_t(i)}{P_{t-1}(i)} - 1 \right)^2 Y_t \right]$$

s.t. $Y_t(i) = \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} Y_t$
 $Y_t = C_t + I_t + \frac{\varrho}{2} Y_t \pi_t^2$, with $I_t \equiv K_{t+1} - (1-\delta)K_t$

Price setting behaviour:

$$(1+\pi_t)\pi_t = \mathbb{E}_t \left(\Lambda_{t,t+1} \frac{Y_{t+1}}{Y_t} (1+\pi_{t+1})\pi_{t+1} \right) - \frac{\epsilon - 1}{\varrho} \left(\frac{\mathcal{M}_t - \mathcal{M}}{\mathcal{M}_t} \right)$$

• Markup $\mathcal{M}_t \equiv \frac{P_t}{(1-\tau)p_t}$ will be important for the effect of MP on FS

$$\max_{N_{t}(j), K_{t}(j)} D_{t}(j) = \frac{P_{t}}{P_{t}} A_{t}(\omega_{t}(j)K_{t}(j))^{\alpha} N_{t}(j)^{1-\alpha} - \frac{W_{t}}{P_{t}} N_{t}(j) + (1-\delta)K_{t}(j) - (1+r_{t}^{c})(K_{t}(j)-K_{t})$$

Defining
$$r_t^k = \frac{p_t}{P_t} \frac{\alpha Y_t(j)}{K_t(j)} - \delta = \frac{p_t}{P_t} \frac{\alpha Y_t}{K_t} - \delta$$
 we obtain:

• Choices of an unproductive firm j with $\omega_t(j) = 0$:

$$\max_{K_t(j)} r_t^q(j) \equiv \frac{D_t(j)}{K_t} - 1 = r_t^c - (r_t^c + \delta) \frac{K_t(j)}{K_t}$$

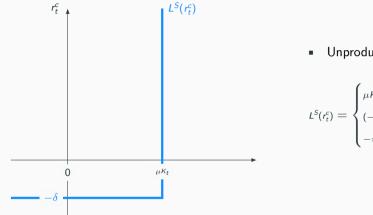
• Choices of a productive firm j with $\omega_t(j) = 1$:

$$\max_{K_t(j)} r_t^q(j) \equiv \frac{D_t(j)}{K_t} - 1 = r_t^c + \left(r_t^k - r_t^c\right) \frac{K_t(j)}{K_t}$$

		ma	

- In the absence of credit frictions,
 - (i) Unproductive firms sell their capital K_t and lend the proceeds on the credit market: $K_t^u = 0$
 - (ii) Productive firms borrow and use the funds to buy $K_t^p K_t > 0$ additional units of capital
 - \Rightarrow The credit market helps reallocate capital: $\mu K_t = (1-\mu)(K_t^p K_t)$
 - $\Rightarrow\,$ Equilibrium of the textbook NK model with a representative firm

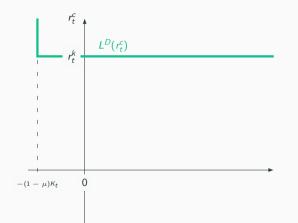
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Unproductive firms' net loan supply

$$L^{S}(r_{t}^{c}) = \begin{cases} \mu K_{t} & \text{for } r_{t}^{c} > -\delta \\ (-\infty, \mu K_{t}] & \text{for } r_{t}^{c} = -\delta \\ -\infty & \text{for } r_{t}^{c} < -\delta \end{cases}$$

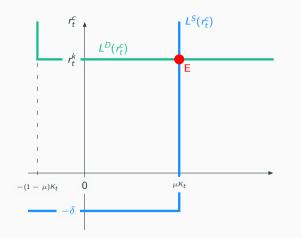




Productive firms' net loan demand

$$\mathcal{L}^{D}(r_{t}^{c}) = \begin{cases} -(1-\mu)\mathcal{K}_{t} & \text{for } r_{t}^{c} > r_{t}^{k} \\ [-(1-\mu)\mathcal{K}_{t}, +\infty) & \text{for } r_{t}^{c} = r_{t}^{k} \\ +\infty & \text{for } r_{t}^{c} < r_{t}^{k} \end{cases}$$



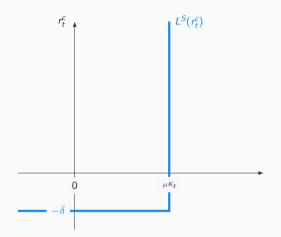


• In E, $r_t^k = r_t^c$ and capital is perfectly reallocated to productive firms:

$$\mu K_t = (1-\mu)(K_t^p - K_t)$$

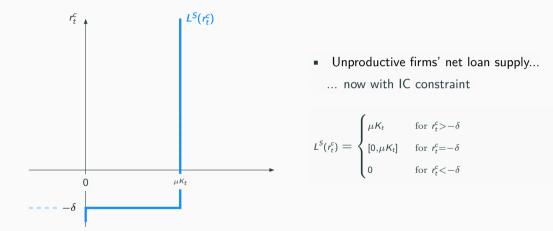
Model boils down to the textbook NK model with one representative firm



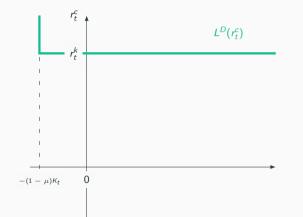


Unproductive firms' net loan supply...



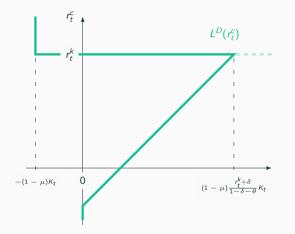






Productive firms' net loan demand...

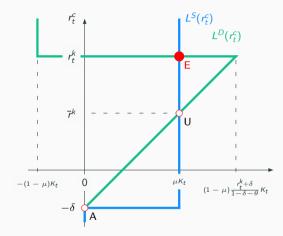




Productive firms' net loan demand...
 ... now with IC constraint

$$\mathbf{L}^{D}(\mathbf{r}_{t}^{c}) = \begin{cases} -(1-\mu)K_{t} & \text{for } \mathbf{r}_{t}^{c} > \mathbf{r}_{t}^{k} \\ \left[-(1-\mu)K_{t}, (1-\mu)\frac{\mathbf{r}_{t}^{k}+\delta}{1-\delta-\theta}K_{t} \right] & \text{for } \mathbf{r}_{t}^{c} = \mathbf{r}_{t}^{k} \\ (1-\mu)\max\{\frac{\mathbf{r}_{t}^{c}+\delta}{1-\delta-\theta}, 0\}K_{t} & \text{for } \mathbf{r}_{t}^{c} < \mathbf{r}_{t}^{k} \end{cases}$$



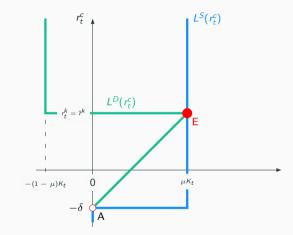


• Equilibrium E is the same as in the frictionless case and textbook model:

 $\mu K_t = (1-\mu)(K_t^p - K_t)$

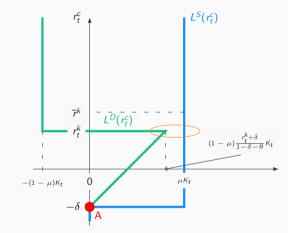
- Aggregate outcome is the same in E and U
- Absence of coordination failure rules out equilibrium A





r^k is the minimum loan rate that ensures that
 <u>all</u> unproductive firms lend (i.e. there is no
 rationing)





- *r*^k is the minimum loan rate that ensures that <u>all</u> unproductive firms lend (i.e. there is no rationing)
- When r^k_t < r^k, there is excess supply and every unproductive firm left out has an incentive to borrow and abscond
- In this case, A (autarky) is the unique equilibrium



Perfect Information Case

- Unproductive firms do not get any loan
- Productive firm *j*s' borrowing limit is given by the incentive compatibility constraint

$$(1-\delta)K_t(j) - \theta(K_t^p - K_t) \le (1+r_t^q(j))K_t = (1+r_t^c)K_t + (r_t^k - r_t^c)K_t(j)$$

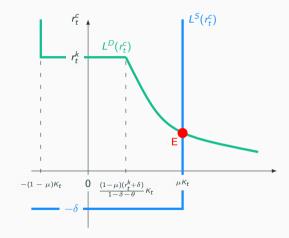
$$\Leftrightarrow K_t(j) - K_t \le \frac{r_t^k + \delta}{1-\delta - \theta + r_t^c - r_t^k}K_t$$

$$\Rightarrow L^D(r_t^c) \equiv (1-\mu)(K_t(j) - K_t) = (1-\mu)\frac{r_t^k + \delta}{1-\delta - \theta + r_t^c - r_t^k}K_t \text{ if } r_t^k \ge r_t^c$$

• Aggregate loan demand monotonically decreases with r_t^c

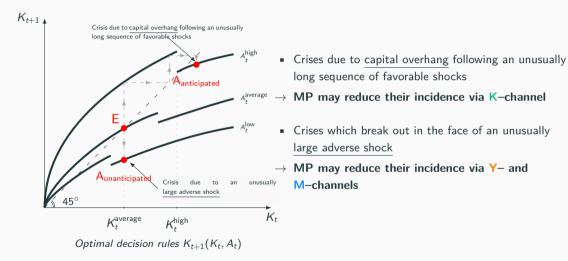


Perfect Information Case



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Two polar types of crisis



Equation Summary

$$1. \quad 1 = \beta \mathbb{E}_{t} \begin{bmatrix} \frac{C_{t+1}^{-\sigma}}{C_{t}} \frac{1+i_{t}}{1+\pi_{t+1}} \end{bmatrix} \qquad 2. \quad 1 = \beta \mathbb{E}_{t} \begin{bmatrix} \frac{C_{t+1}^{-\sigma}}{C_{t}} (1+r_{t+1}^{q}) \end{bmatrix} \\
3. \quad \chi N_{t}^{\varphi} C_{t}^{\sigma} = \frac{\epsilon}{\epsilon-1} \frac{(1-\alpha)Y_{t}}{\mathcal{M}_{t}N_{t}} \qquad 4. \quad r_{t}^{q} + \delta = \frac{\epsilon}{\epsilon-1} \frac{\alpha Y_{t}}{\mathcal{M}_{t}K_{t}} \\
5. \quad Y_{t} = C_{t} + X_{t} - \frac{\varrho}{2}\pi_{t}^{2} \qquad 6. \quad K_{t+1} = X_{t} + (1-\delta)K_{t} \\
7. \quad Y_{t} = A_{t} (\omega_{t}K_{t})^{\alpha} N_{t}^{1-\alpha} \qquad 8. \quad \omega_{t} = \begin{cases} 1 & \text{if } r_{t}^{q} \ge \frac{\mu(1-\theta)-\delta}{1-\mu} \\ 1-\mu & \text{otherwise} \end{cases} \\
9. \quad (1+\pi_{t})\pi_{t} = \beta \mathbb{E}_{t} \left(\frac{C_{t+1}^{-\sigma}}{C_{t}^{-\sigma}} \frac{Y_{t+1}}{Y_{t}} (1+\pi_{t+1})\pi_{t+1} \right) - \frac{\epsilon-1}{\varrho} \left(1 - \frac{\epsilon}{\epsilon-1} \cdot \frac{1}{\mathcal{M}_{t}} \right) \\
10. \quad 1 + i_{t} = \frac{1}{\beta} (1+\pi_{t})^{\phi_{\pi}} \left(\frac{Y_{t}}{Y_{t}} \right)^{\phi_{Y}} \end{cases}$$

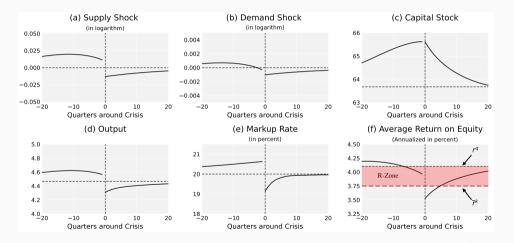
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Parametrisation

Parameter	Target	Value
Preferences		
β	4% annual real interest rate	0.989
σ	Logarithmic utility on consumption	1
φ	Inverse Frish elasticity equals 2	0.5
χ	Steady state hours equal 1	0.81
Technology	and price setting	
α	64% labor share	0.36
δ	6% annual capital depreciation rate	0.015
ρ	Same slope of the Phillips curve as with Calvo price setting	58.22
ϵ	20% markup rate	6
Aggregate	TFP (supply) shocks	
ρ_a	Standard persistence	0.95
σ_a	Volatility of inflation and output in normal times (in $\%$)	0.81
Aggregate	Demand shocks	
ρ_z	Standard persistence	0.95
σ_z	Volatility of inflation and output in normal times (in $\%$)	0.16
Interest rat	e rule	
ϕ_{π}	Response to inflation under TR93	1.5
ϕ_y	Response to output under TR93	0.125
Financial F	rictions	
μ	Productivity falls by 1.8% due to financial frictions during a crisis	0.05
θ	The economy spends 10% of the time in a crisis	0.52

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Anatomy of the average crisis



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- No credit frictions: SIT eliminates simultaneously inefficient fluctuations in prices and output gap and achieves the first best allocation – "divine coincidence" (Blanchard and Galí (2007))
- Credit frictions: SIT does not deliver the first best allocation \Rightarrow may not be optimal anymore
- Should central banks deviate from price stability to promote financial stability?
- To answer this question, we study:
 - The trade-off between price and financial stability
 - Compare welfare under SIT with that under alternative policy rules: (i) Taylor-type rules, (ii) Taylor-type rules augmented with the yield gap, (iii) regime-contingent backstop rules

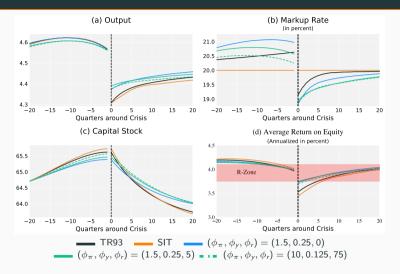


Welfare and crisis statistics under alternative monetary policy regimes

	Rule			Model with Financial Frictions					Frictionless
	parameters			Time in	Length	Output	$Std(\pi_t)$	Welfare	Welfare
	ϕ_{π}	ϕ_y	ϕ_r	Crisis/Stress (in %)	(quarters)	Loss (in %)	(in pp)	Loss (in %)	Loss (in %)
				Stand	lard Taylo	or-type Ru	iles		
(1)	1.5	0.125	-	[10]	4.8	6.6	1.2	0.82	0.56
(2)	1.5	0.250	_	7.2	4.0	5.4	1.8	1.48	1.21
(3)	1.5	0.375	-	4.1	3.1	4.4	2.5	3.10	2.07
(4)	2.0	0.125	_	9.7	5.0	7.2	0.6	0.41	0.17
(5)	2.5	0.125	-	9.6	5.1	7.5	0.5	0.31	0.08
					SI	г			
(6)	$+\infty$	-	-	9.4	5.1	8.1	0	0.23	0.00
				Augme	nted Tay	lor-type F	Rules		
(7)	1.5	0.125	5.0	5.4	3.9	5.5	1.16	0.65	-
(8)	5.0	0.125	5.0	8.8	5.0	7.4	0.18	0.22	_
(9)	5.0	0.125	25.0	6.9	4.7	6.6	0.19	0.18	-
(10)	10.0	0.125	75.0	6.3	4.6	6.4	0.09	0.16	-
					Backsto	p Rules			
(11)	1.5	0.125	-	15.5	-	-	1.21	0.56	-
(12)	$+\infty$	_	-	17.1	-	-	0.50	0.10	-

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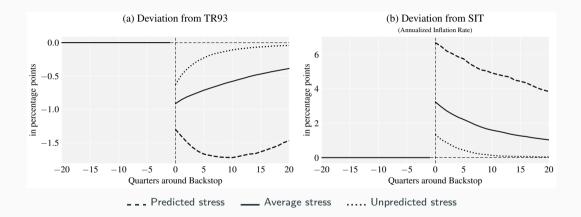
Why do Taylor rules improve FS over SIT?



• Short run: The Taylor-type rules cushion better the fall in r_t^k in the face of adverse shocks

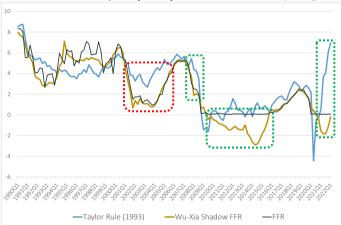
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"Backstop rules" and normalisation paths



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Deviation from Taylor (1993) rule and shadow policy rate



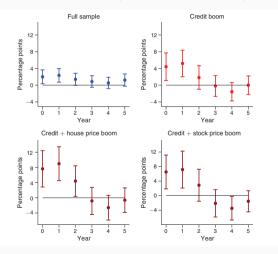
Deviation from Taylor (1993) rule and shadow policy rate

Source: Federal Reserve Bank of Atlanta



Schularick at al (2021)

Effect on annual crisis probability of an unexpected 1 pp policy rate hike



"Based on the near-universe of advanced economy financial cycles since the nineteenth century, we show that **discretionary** leaning against the wind policies during credit and asset price booms are more likely to trigger crises than prevent them".

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